

Journal club

Droplet polydispersity and shape fluctuations in AOT [bis(2-ethylhexyl)sulfosuccinate sodium salt] microemulsions studied by contrast variation small -angle neutron scattering

L. Arleth and J. S. Pedersen, *Phys. Rev. E* **63**, 61406 (2001)

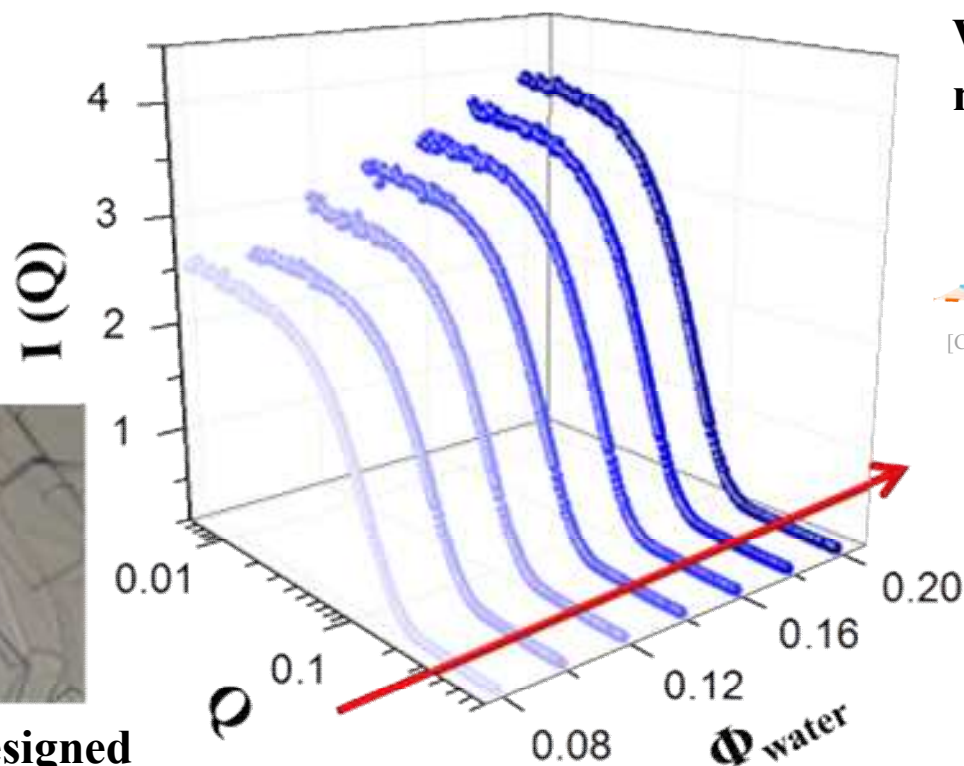
Yoonnam Jeon (2016. 01. 23)

RELATED WORK Conformation change by adding water

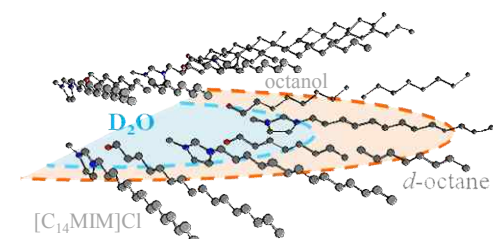


**Molecular designed
single crystal**

Kang et. al.,
J. Phys. Chem. C **117**, 14332 (2013)



Water in oil microemulsion



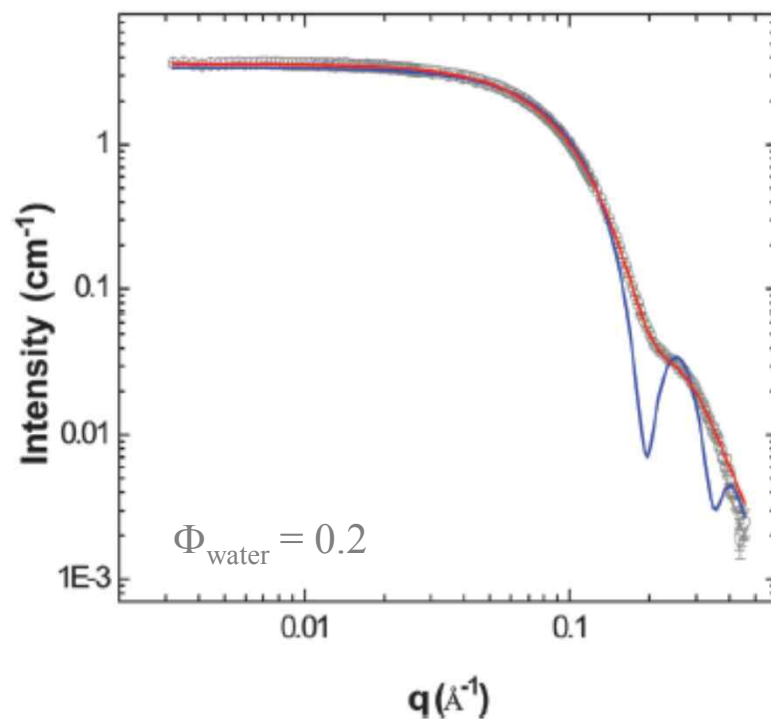
Kang et. al.,
Phys. Chem. Chem. Phys.
17, 27833 (2015)

※ No direct evidence of ellipsoidal structure



Model fitting : sphere

RELATED WORK Highly polydispersed microemulsion



Model	Volume density	Core radius (Å)	Shell thickness (Å)	Polydispersity
Mono	0.021	8	15	0
Poly-core	0.035	10	9	0.37

Kang et. al., *Phys. Chem. Chem. Phys.*
17, 27833 (2015)

Question

0.37 polydispersity is quite high

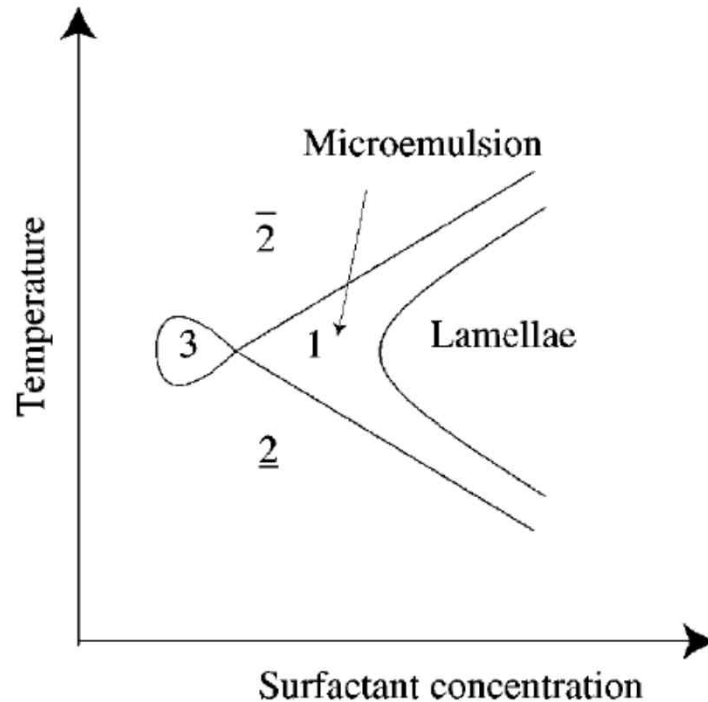
SANS :

Ellipsoids is equivalent to that of a distribution of **poly disperse spheres**

Arleth and Pedersen,
Phys. Rev. E **63**, 061406 (2001)

INTRODUCTION

fish-diagram



Microstructure of microemulsions

Varies a lot depending upon

- actual system
- composition
- temperature
- additives



Simplest system

Water/alkane/ C_iE_j (nonionic surfactant)

Water/alkane/AOT(ionic surfactant) – less simple in practice

Aim To get information about the polydispersity and shape fluctuations of the droplets

INTRODUCTION

Polydispersity (σ / R_{av})

- AOT/water/hexane : 12% (Ricka et. al. 1991)
- AOT/water/iso-octane : 19% (Christ and Schurtenberger et. al. 1994)
- AOT/water/decane : 10% (Christ and Schurtenberger et. al. 1994)

- Theoretical prediction : 0.1 – 0.2
- Experimental reports : 10 – 45% (most often : 15 – 25%)

For nonionic surfactant (C_iE_j)

- polydispersity is independent of alkane type (Pedersen and coworkers, 1996)

➡ **Aim** The polydispersity and shape fluctuations using SANS

SANS :

Ellipsoids is equivalent to that of a distribution of **poly disperse spheres**

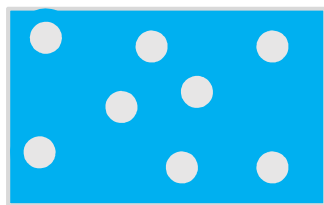
EXPERIMENTS

➤ Sample preparation

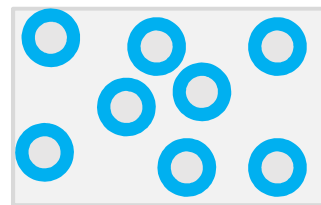
- AOT + water ~ 5% (water / AOT = 38 molar ratio)
- Alkanes : decane & iso-octane

➤ Small Angle Neutron Scattering (SANS)

- Risø National Laboratory
- $0.004 < q < 0.26 \text{ \AA}^{-1}$
- Contrast matching exp. mixing with *h*- and *d*-alkanes



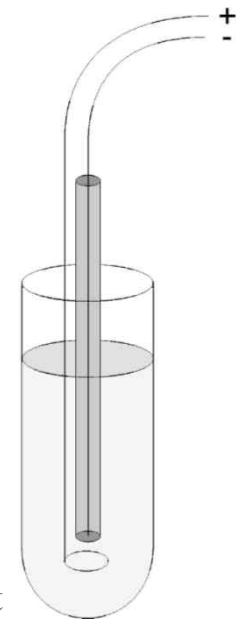
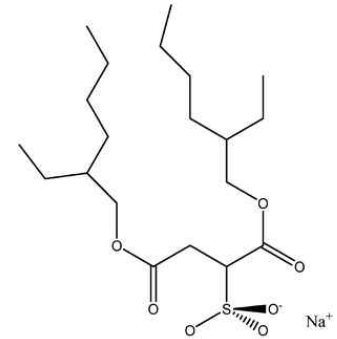
h-alkane



d-alkane

➤ Conductivity measurement

- CDM80 conductivity meter



cathode and anode : Pt

CONDUCTIVITY MEASUREMENT Transition of conductivity

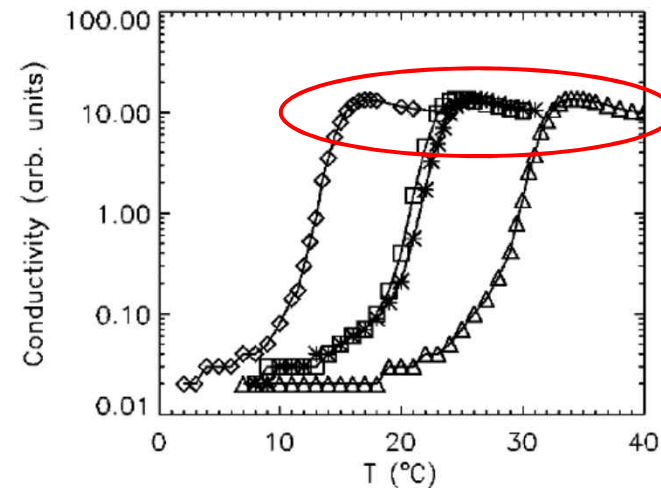
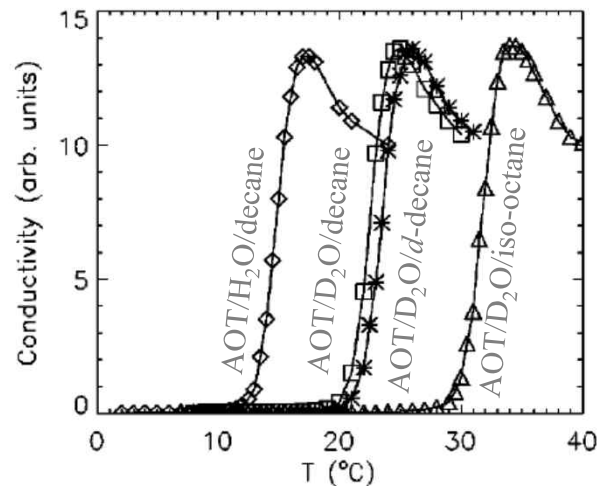
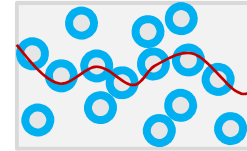
➤ Temperature dependent conductivity

- Well known : AOT/water/alkane

➡
high T

- larger aggregates of droplets are formed

- allow the counterions of the AOT to move round

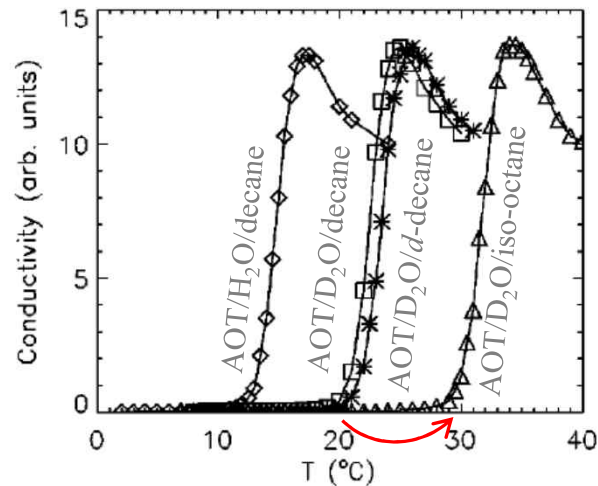


➤ **Slow decreased conductivity** Have not been able to find such an effect

➤ **Main interest : Position of transition**

- From w/o microemulsions to microemulsions with connected water domains

CONDUCTIVITY MEASUREMENT Transition of conductivity



Sample	$T_{off-set}$ (°C)	T_{max} (°C)
AOT/H ₂ O/ <i>h</i> -dec	12	17
AOT/D ₂ O/ <i>h</i> -dec	19	25
AOT/D ₂ O/ <i>d</i> -dec	20	26
AOT/D ₂ O/ <i>h</i> -iso	28	34

jump : 9°C

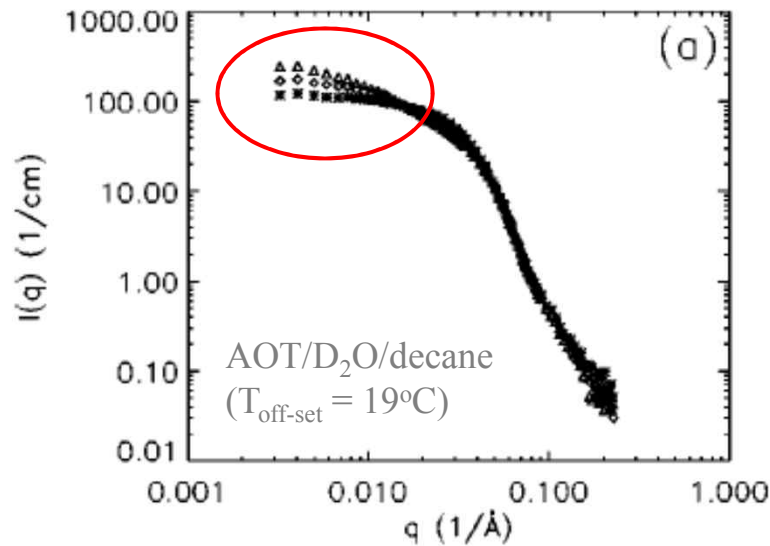
➤ Conductivity jump by changing solvent (decane → isooctane)

- agreement with former measurement
- connected to the **decreasing penetration of solvent** into the surfactant layer with **increasing molecular weight** ($m_{decane} > m_{isooctane}$)

➤ Conductivity jump with heavy water

- suggest : water structure plays a very import role in the microemulsion phase behavior

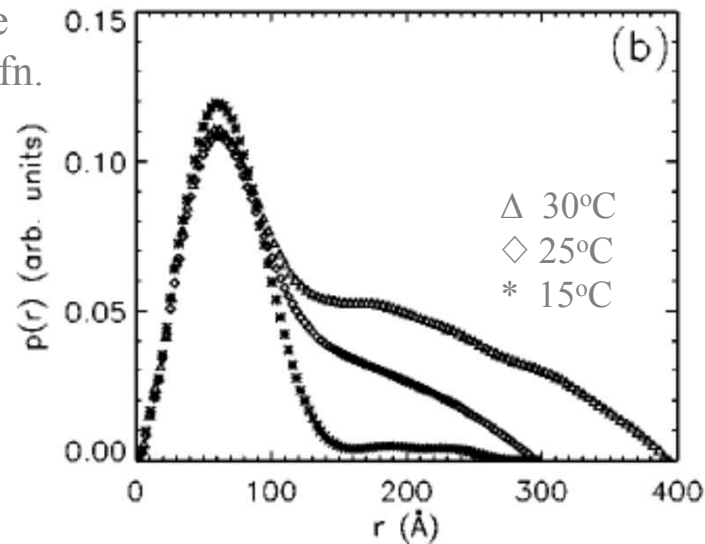
ANALYSIS OF SANS Temperature dependent pair distribution fn.



➤ **Increased scattering at low q with increasing temp.**

- size of the droplets increases

pair-distance
distribution fn.



➤ **For the same contrast**

- spherical : give rise to a bell shaped curve

- elongated (or polydisperse) :

$p(r)$ will have a tail and go to zero at higher r

ANALYSIS OF SANS Form and Structure factors

➤ Form factor

- sphere

$$F_1(qR) = 3 \frac{\sin(qR) - qR \cos(qR)}{(qR)^3}$$

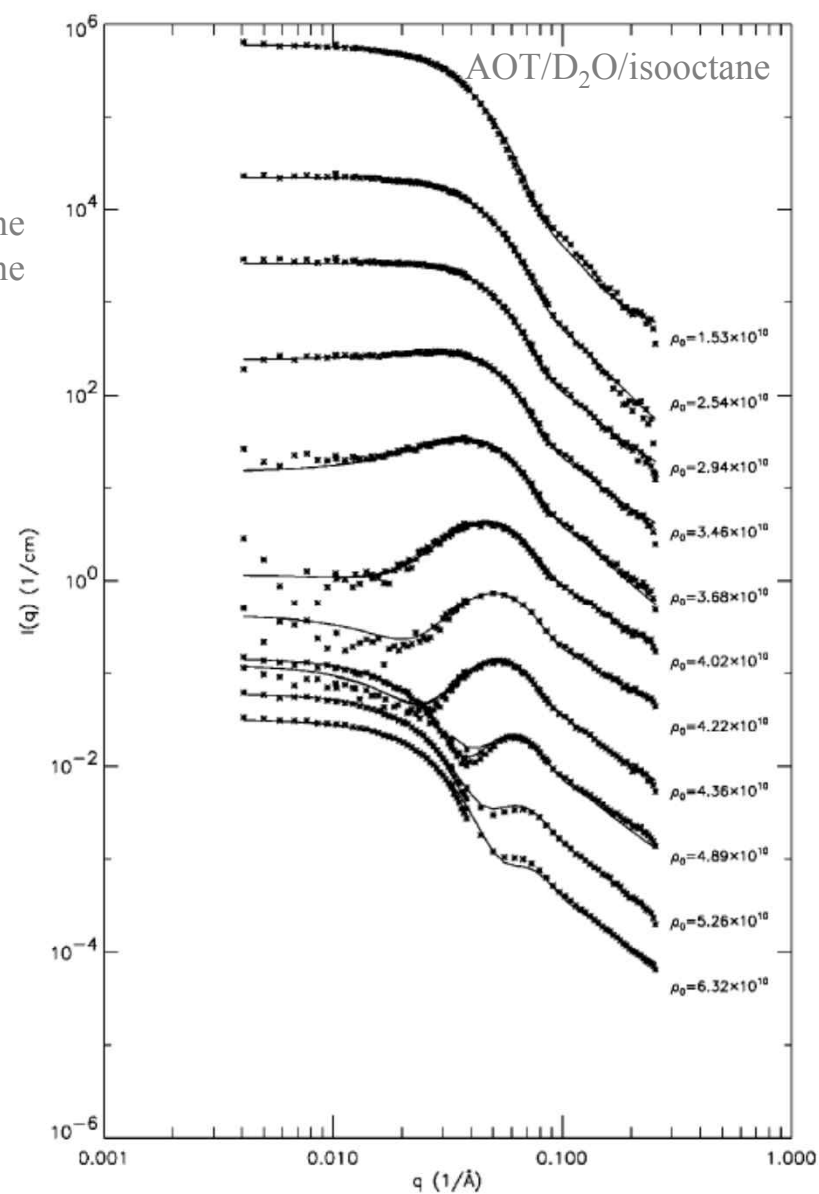
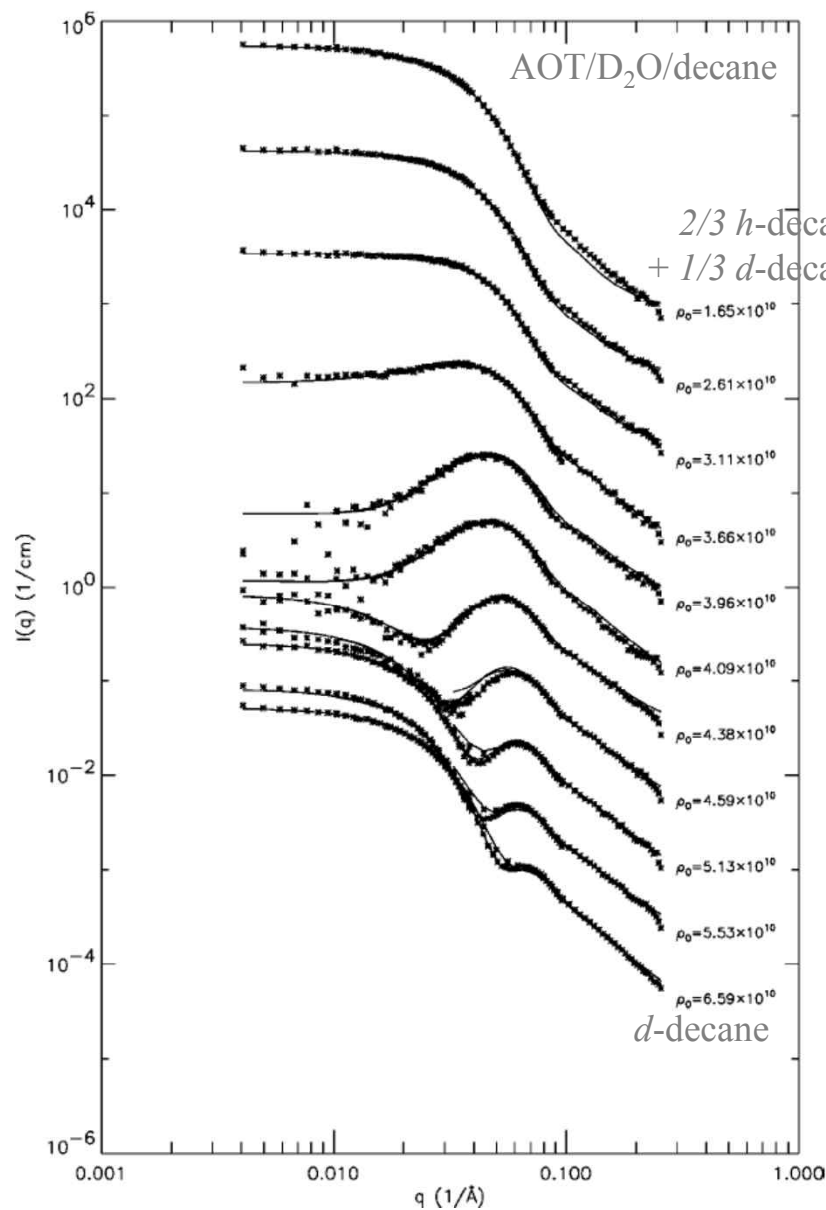
- ellipsoid

$$\langle F(q)^2 \rangle_0 = \int_0^{\pi/2} \left(V_0(\rho_c - \rho_s) F_1(qR_c \sqrt{\sin^2 \theta + \varepsilon_c^2 \cos^2 \theta}) (V_c + V_s)(\rho_s - \rho_{\text{solvent}}) \right) \times F_1(qR_s \sqrt{\sin^2 \theta + \varepsilon_s^2 \cos^2 \theta})^2 \sin \theta d\theta$$

➤ Structure factor

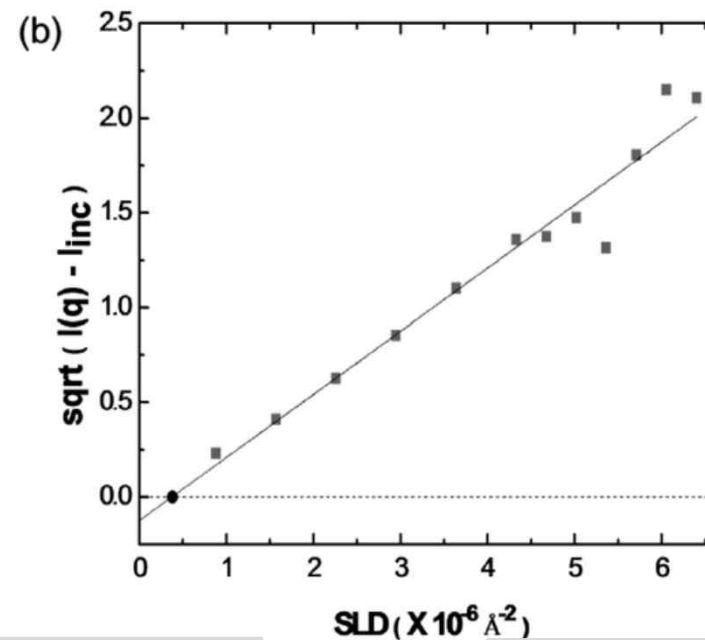
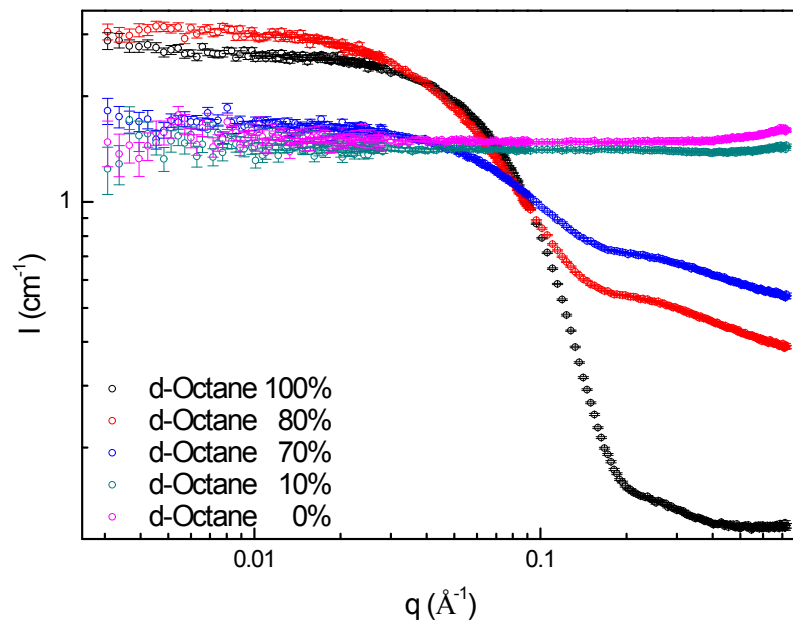
- Did not use the model that includes stickiness of the spheres
- Structure factor for a distribution of polydisperse hard spheres

ANALYSIS OF SANS Contrast matching exp.



ANALYSIS OF SANS Contrast matching exp.

(IL : octanol : water = 1 : 4 : 2)

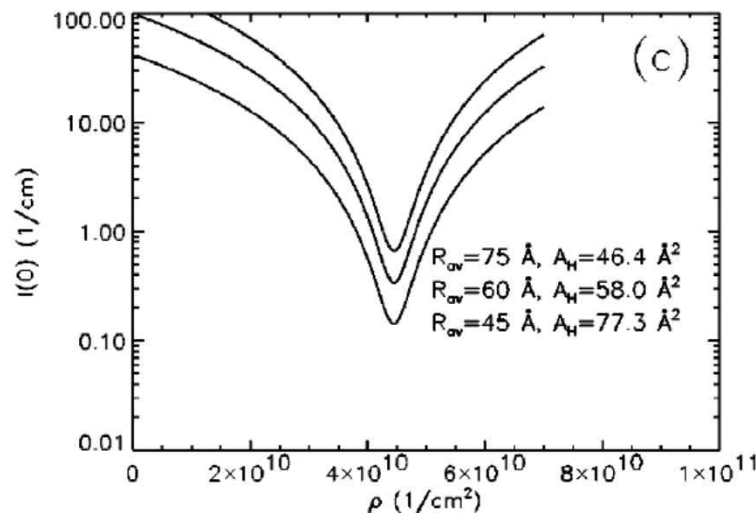
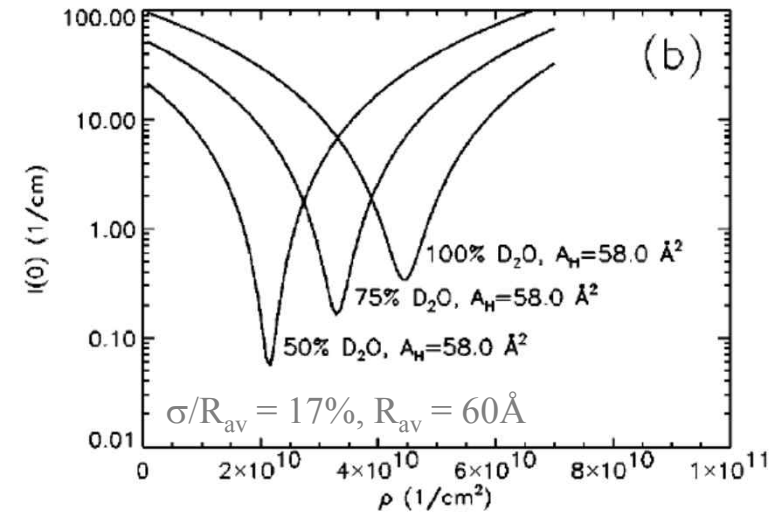
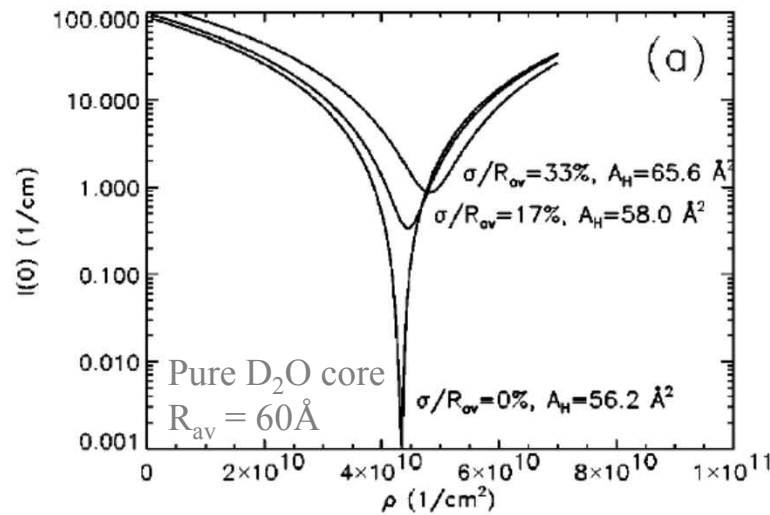


→ $\rho_{\text{shell}} \sim 0.7 \pm 0.1 \text{ E-06 (}\text{\AA}^{-2}\text{)}$

Kang et. al., *Phys. Chem. Chem. Phys.* **17**, 27833 (2015)

RESULTS & DISCUSSION Contrast matching point

- **Model calculation of $I(0)$** $f(0) = V_c(\rho_c - \rho_s) + (V_c + V_s)(\rho_s - \rho_{\text{solvent}})$: form factor



If the droplets are monodisperse
(same composition and same ρ_c, ρ_s)

➡ matched out at same ρ_{solvent}

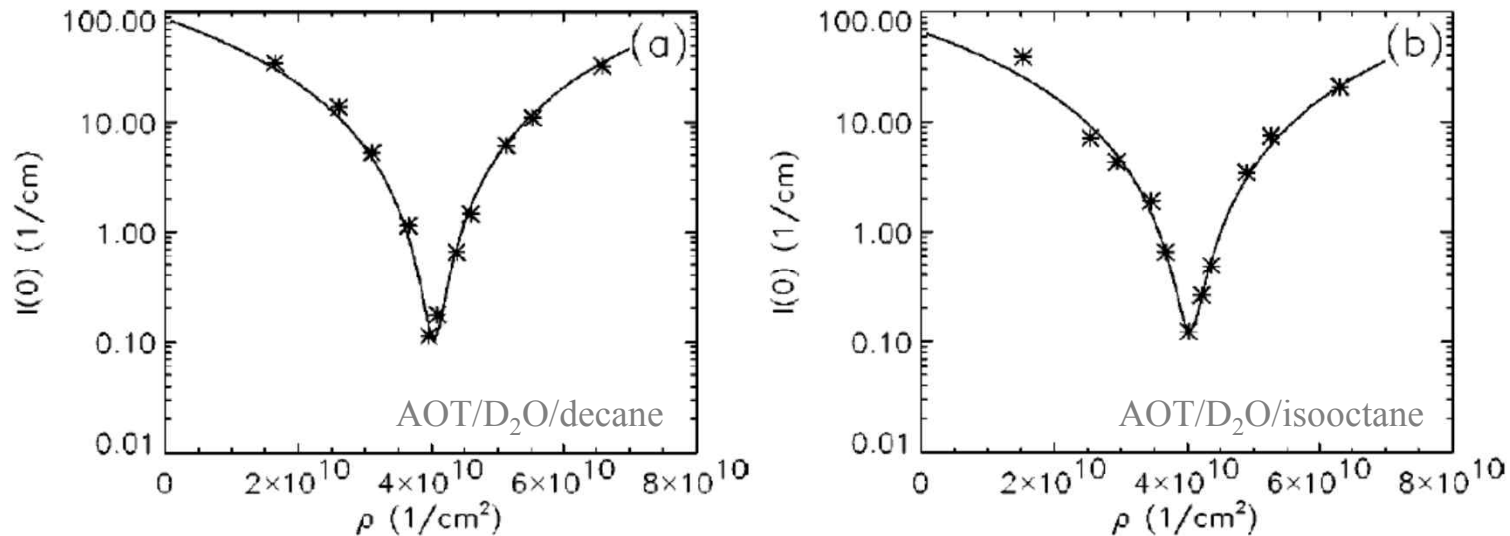
Depth : Mainly determined by σ/R

Position : Mainly determined by composition
of core

Absolute intensity : Mainly determined by
mean radius

RESULTS & DISCUSSION Contrast matching point

➤ Experimental values of $I(0)$ with least-squares fit

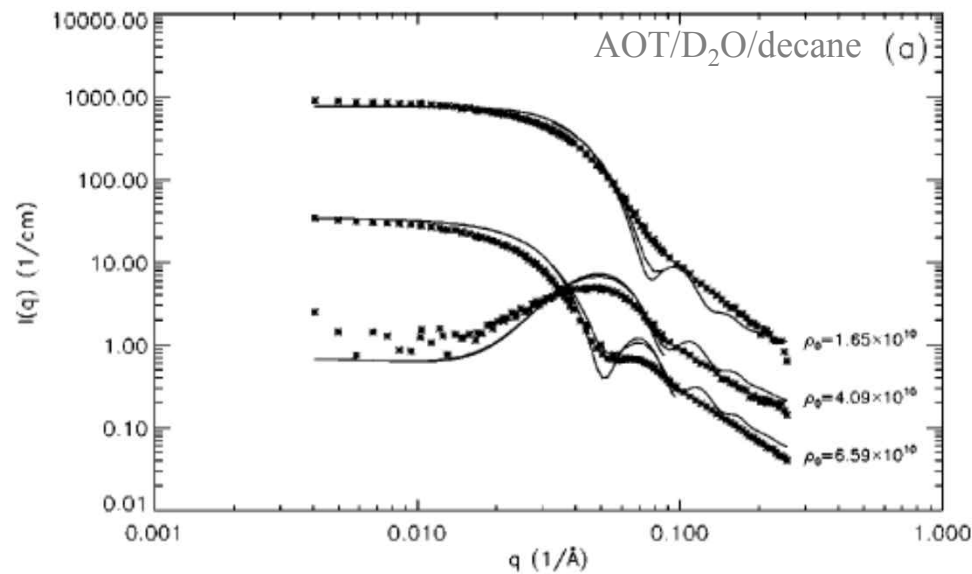


Parameter	AOT/D ₂ O/dec	AOT/D ₂ O/iso
R_{av} (Å)	61.91 ± 1.1	56.34 ± 1.0
σ/R_{av}	0.094 ± 0.009	0.120 ± 0.010
Purity _{D₂O}	0.928 ± 0.004	0.923 ± 0.004
A_{head} (Å ²)	54.9 ± 1.2	60.7 ± 1.2

Comparable with the value determined by contrast variation light scattering

- Hofmeier and coworkers, $\sigma/R_{av} = 12\%$ in the AOT/water/hexane
- Christ and Schurtenberger, $\sigma/R_{av} = 10\%$ in the AOT/water/decane

RESULTS & DISCUSSION SANS data fitting

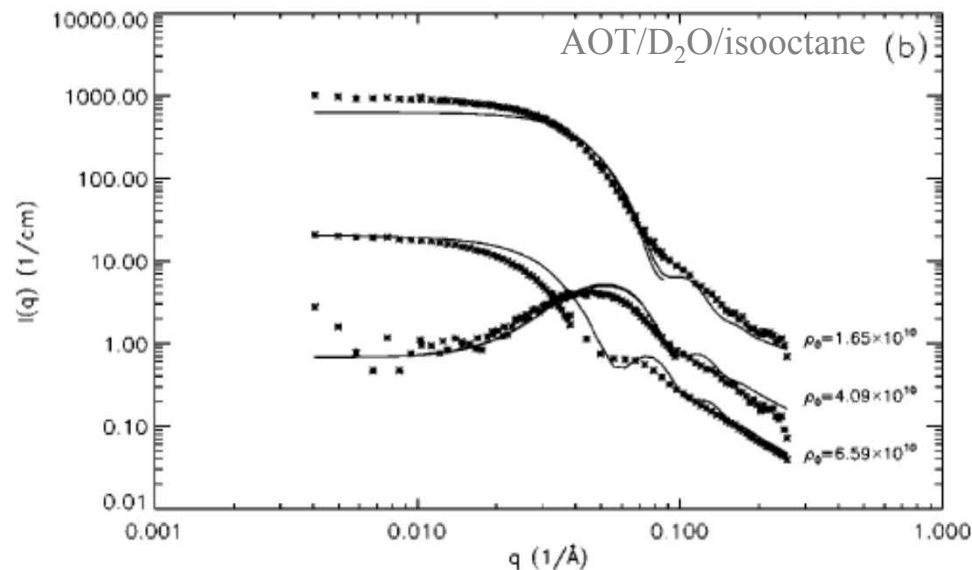


data & model fitted to the $I(0)$

At higher q
modeled $I(0)$ is much more
oscillatory than the experimental $I(q)$

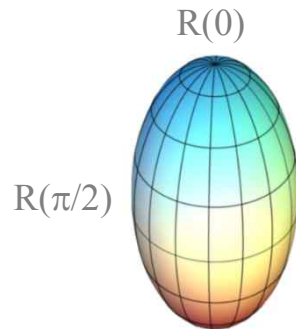
Suggest

The droplets are **more polydisperse**
than indicated by the $I(0)$ data
or
they are **nonspherical**



RESULTS & DISCUSSION Size of shape fluctuation

➤ Angular dependent radius



with, fluctuation amplitude u_{lm} , spherical harmonics Y_{lm}

$$R(\Omega) = R_{av} [1 + \Sigma \underline{u_{lm} Y_{lm}}(\Omega)]$$

deviation from sphere

$$\left\{ \begin{array}{l} u_{00} Y_{00}(\Omega) : \text{polydispersity term} \\ u_{2m} Y_{2m}(\Omega) : \text{first order shape fluctuation term} \end{array} \right.$$

$$\rightarrow \left\{ \begin{array}{l} \sigma / R_{av} \sim \sqrt{\frac{\langle |u_{00}|^2 \rangle}{4\pi}} \\ \varepsilon \text{ (axis ratio)} = \frac{R(0)}{R(\pi/2)} = \frac{1 + u_{00}/2\sqrt{\pi} + 10\sqrt{5/\pi}u_{20}/4}{1 + u_{00}/2\sqrt{\pi} - 5\sqrt{5/\pi}u_{20}/4} \end{array} \right.$$

Safran, *J. Chem. Phys.* **78**, 2073 (1983)

RESULTS & DISCUSSION Determination of the bending constant

$$\langle |u_{00}|^2 \rangle = \frac{k_B T}{12k \left[8(R/R_0)(k + k'/2) + 6k \right]}$$

$$\langle |u_{20}|^2 \rangle = \frac{k_B T}{16(R/R_0)(k + k'/2) \left[12k \right]}$$

Safran, *Phys. Rev. A* **43**, 2903 (1991)

where

k : bending elastic constant

k' : Gaussian bending elastic constant of the film

R_0 : droplet radius at the emulsification boundary

σ/R_{av}	ϵ	$\langle u_{00} ^2 \rangle$	$\langle u_{20} ^2 \rangle$	$\kappa (k_B T)$	$\bar{\kappa} (k_B T)$	System
0.157*	1.56*	0.310	0.0133	3.4 ± 0.2	-5.9 ± 0.4	Present measurements
0.156*	1.72*	0.306	0.0201	2.35 ± 0.1	-3.8 ± 0.2	AOT/D ₂ O/decane
						AOT/D ₂ O/iso-octane
0.22*	1.47	0.61	0.011*	3.9	-7.2	AOT/D ₂ O/decane
				(3.8)	(-7.5)	[14]
0.17	2.5	0.34	0.062	0.92*	-0.38*	C ₁₀ E ₅ /D ₂ O/octane
(0.20)						[57]
0.17	2.2	0.29	0.043	1.25*	-0.80*	C ₁₀ E ₅ /D ₂ O/ <i>n</i> -dodecane
(0.15)						[15]

¹⁴Arleth and Pedersen, *Phys. Rev. E* **63**, 61406 (2001), ⁵⁷Safran and coworkers, *Phys. Rev. Lett.* **65**, 3348 (1990)

¹⁵Hellweg and Lagevin, *Phys. Rev. E* **57**, 6825 (1998)