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## A comparative study of confined organic monolayers by Raman scattering and sum-frequency spectroscopy

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### Abstract

The structure of a Langmuir–Blodgett (LB) monolayer of Zn arachidate at the solid–solid interface has been studied by Raman scattering and sum-frequency (SF) spectroscopy. The monolayer was confined in the contact between a  $\text{CaF}_2$  prism and a  $\text{MgF}_2$  lens at an average pressure of 60 MPa. This is the first report of an unenhanced Raman spectrum of an organic monolayer at the solid–solid interface. The Raman and SF spectra both show that the deposited monolayer is conformationally ordered and that the monolayer retains this order when placed between the prism and the lens. The relative intensity of the Raman spectra of the Zn arachidate monolayer at the  $\text{CaF}_2$ /air and  $\text{CaF}_2$ / $\text{MgF}_2$  interfaces can be explained in terms of the strength of the interfacial electric fields. The relative intensities of the SF spectra at the two interfaces cannot be interpreted in this manner. Deviations from the expected intensities are discussed in terms of structural changes in the monolayer. © 2000 Elsevier Science B.V. All rights reserved.

*Keywords:* Raman scattering; Sum-frequency spectroscopy; Monolayer; Tribology; Total internal reflection

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# Fresnel coefficients

- $K_{p,x} = \frac{2n_i \cos\theta_i \cos\theta_t}{n_t \cos\theta_i + n_i \cos\theta_t}$
- $K_{s,y} = \frac{2n_i \cos\theta_i}{n_i \cos\theta_i + n_t \cos\theta_t}$
- $K_{p,z} = \frac{2n_i \cos\theta_i \sin\theta_t}{n_t \cos\theta_i + n_i \cos\theta_t} \left(\frac{n_t}{n'}\right)^2$

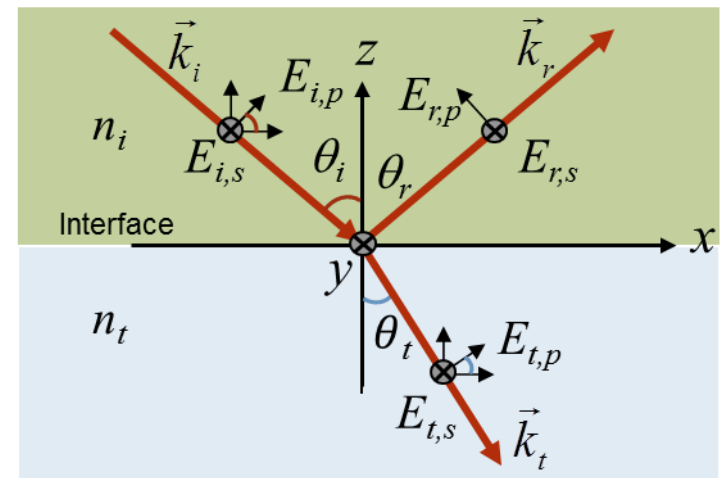
the refractive indices:

$n_i \rightarrow$  of the incident media

$n_t \rightarrow$  of the transmitted media

$n' \rightarrow$  of the monolayer

Snell's Law:  $\sin\vartheta_t = (n_i/n_t)\sin\vartheta_i$ .



# Fresnel coefficients

- $$L_{xx} = \frac{E_{t,p} \cos\theta_t}{E_{i,p} \cos\theta_i} = t_p \frac{\cos\theta_t}{\cos\theta_i} = \frac{2n_i \cos\theta_i}{n_i \cos\theta_t + n_t \cos\theta_i} \frac{\cos\theta_t}{\cos\theta_i} = \frac{2n_i \cos\theta_t}{n_i \cos\theta_t + n_t \cos\theta_i} \Rightarrow$$

- $$L_{yy} = t_s = \frac{2n_i \cos\theta_i}{n_i \cos\theta_i + n_t \cos\theta_t}$$

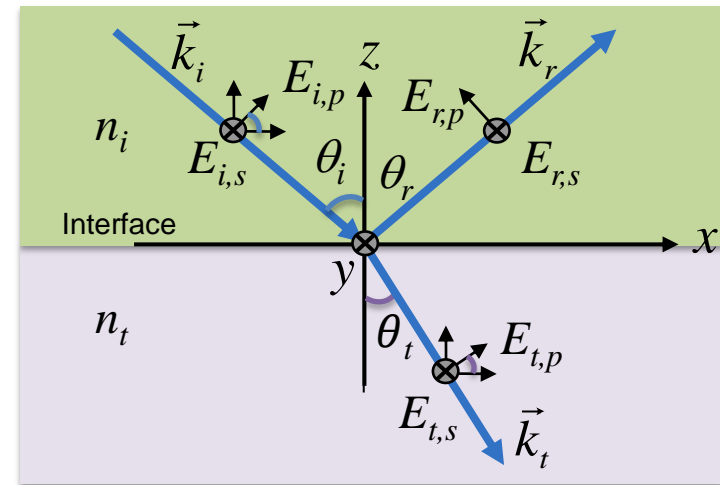
- $$L_{zz} = \frac{E_{t,p} \sin\theta_t}{E_{i,p} \sin\theta_i} \cdot \zeta = t_p \frac{\sin\theta_t}{\sin\theta_i} \cdot \zeta = \frac{2n_i \cos\theta_i}{n_i \cos\theta_t + n_t \cos\theta_i} \frac{\sin\theta_t}{\sin\theta_i} \cdot \zeta \Rightarrow$$

$$\therefore n_i \sin\theta_i = n_t \sin\theta_t$$

- $$L_{xx} = \frac{2n_i \cos\theta_t}{n_i \cos\theta_t + n_t \cos\theta_i}$$

- $$L_{yy} = \frac{2n_i \cos\theta_i}{n_i \cos\theta_i + n_t \cos\theta_t}$$

- $$L_{zz} = \frac{2n_t \cos\theta_i \sin\theta_t}{n_i \cos\theta_t + n_t \cos\theta_i} \left(\frac{n_i}{n}\right)^2$$



# Fresnel coefficients at TIR

$$\therefore \cos\theta_t = \sqrt{1 - \sin^2\theta_t} = \sqrt{1 - \left(\frac{n_i}{n_t}\right)^2 \sin^2\theta_i} = \frac{\sqrt{n_{ti}^2 - \sin^2\theta_i}}{n_{ti}} = \frac{i\sqrt{\sin^2\theta_i - n_{ti}^2}}{n_{ti}}$$

$$K_{p,x} = \frac{2n_i \cos\theta_t}{n_t \cos\theta_i + n_i \cos\theta_t} \Rightarrow$$

$$\sin\theta_t = \left(\frac{n_i}{n_t}\right) \sin\theta_i$$

$$Re(K_{p,x}) = \frac{2(\sin^2\theta_i - n_{ti}^2)}{n_{ti}^4 \cos^2\theta_i + \sin^2\theta_i - n_{ti}^2}, Im(K_{p,x}) = \frac{2n_{ti}^2 \cos\theta_i (\sin^2\theta_i - n_{ti}^2)^{1/2}}{n_{ti}^4 \cos^2\theta_i + \sin^2\theta_i - n_{ti}^2}$$

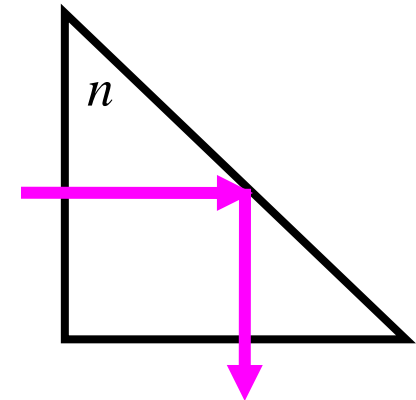
$$n_{ti} = \frac{n_t}{n_i}$$

$$K_{s,y} = \frac{2n_i \cos\theta_i}{n_i \cos\theta_i + n_t \cos\theta_t} \Rightarrow$$

$$Re(K_{s,y}) = \frac{2 \cos^2\theta_i}{1 - n_{ti}^2}, Im(K_{s,y}) = \frac{-2 \cos\theta_i (\sin^2\theta_i - n_{ti}^2)^{1/2}}{1 - n_{ti}^2}$$

$$K_{p,z} = \frac{2n_i \cos\theta_i}{n_t \cos\theta_i + n_i \cos\theta_t} \left(\frac{n_t}{n_i}\right)^2 \Rightarrow$$

$$Re(K_{p,z}) = \frac{2n_{ti}^2 \cos^2\theta_i}{n_{ti}^4 \cos^2\theta_i + \sin^2\theta_i - n_{ti}^2}, Im(K_{p,z}) = \frac{-2 \cos\theta_i (\sin^2\theta_i - n_{ti}^2)^{1/2}}{n_{ti}^4 \cos^2\theta_i + \sin^2\theta_i - n_{ti}^2}$$



$$K_{p,x} = \frac{2n_i \cos \theta_t}{n_t \cos \theta_i + n_i \cos \theta_t} = \frac{2i \sqrt{\sin^2 \theta_i - n_{ti}^2}}{n_{ti}^2 \cos \theta_i + i \sqrt{\sin^2 \theta_i - n_{ti}^2}} = \frac{2i \sqrt{\sin^2 \theta_i - n_{ti}^2} (n_{ti}^2 \cos \theta_i - i \sqrt{\sin^2 \theta_i - n_{ti}^2})}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}$$

$$\Rightarrow \operatorname{Re}(K_{p,x}) = \frac{2(\sin^2 \theta_i - n_{ti}^2)}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}, \quad \operatorname{Im}(K_{p,x}) = \frac{2n_{ti}^2 \cos \theta_i (\sin^2 \theta_i - n_{ti}^2)^{1/2}}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}$$

$$K_{s,y} = \frac{2n_i \cos \theta_i}{n_i \cos \theta_i + n_t \cos \theta_t} = \frac{2n_i \cos \theta_i}{n_i \cos \theta_i + n_t \frac{i \sqrt{\sin^2 \theta_i - n_{ti}^2}}{n_{ti}}} = \frac{2 \cos \theta_i}{\cos \theta_i + i \sqrt{\sin^2 \theta_i - n_{ti}^2}} \times \frac{\cos \theta_i - i \sqrt{\sin^2 \theta_i - n_{ti}^2}}{\cos \theta_i - i \sqrt{\sin^2 \theta_i - n_{ti}^2}} =$$

$$= \frac{2 \cos \theta_i (\cos \theta_i - i \sqrt{\sin^2 \theta_i - n_{ti}^2})}{\cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}$$

$$\Rightarrow \operatorname{Re}(K_{s,y}) = \frac{2 \cos^2 \theta_i}{1 - n_{ti}^2}, \quad \operatorname{Im}(K_{s,y}) = \frac{-2 \cos \theta_i (\sin^2 \theta_i - n_{ti}^2)^{1/2}}{1 - n_{ti}^2}$$

$$K_{p,z} = \frac{2n_i \cos \theta_i}{n_t \cos \theta_i + n_i \cos \theta_t} \left(\frac{n_t}{n'}\right)^2 = \left(\frac{n_t}{n'}\right)^2 \frac{2n_i \cos \theta_i}{n_t \cos \theta_i + n_i \frac{i \sqrt{\sin^2 \theta_i - n_{ti}^2}}{n_{ti}}} = \left(\frac{n_t}{n'}\right)^2 \frac{2 \cos \theta_i (n_{ti}^2 \cos \theta_i - i \sqrt{\sin^2 \theta_i - n_{ti}^2})}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}$$

$$\Rightarrow \operatorname{Re}(K_{p,z}) = \frac{2n_{ti}^2 \cos^2 \theta_i}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}, \quad \operatorname{Im}(K_{p,z}) = \frac{-2 \cos \theta_i (\sin^2 \theta_i - n_{ti}^2)^{1/2}}{n_{ti}^4 \cos^2 \theta_i + \sin^2 \theta_i - n_{ti}^2}$$

$$L_{s,y}^r = 4\pi i \frac{\omega_{sum}}{c} \frac{1}{n_i \cos \theta_r + n_t \cos \theta_t}$$

$\theta_r$  is the angle of emission of the SF light

Above the critical angle, the real and imaginary parts of

$L_{s,y}$  are given by:

$$Re(L_{s,y}^r) = 4\pi \frac{\omega_{sum}}{c} \frac{(\sin^2 \theta_r - n_{ti}^2)^{1/2}}{n_{ti}(1 - n_{ti}^2)}$$

$$Im(L_{s,y}^r) = 4\pi \frac{\omega_{sum}}{c} \frac{\cos \theta_i}{n_{ti}(1 - n_{ti}^2)}$$

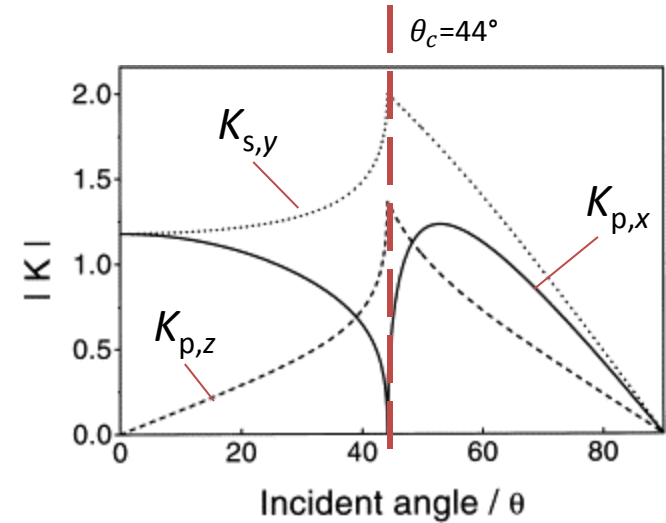
$$L_{s,y}^r = 4\pi i \frac{\omega_{sum}}{c} \frac{1}{n_i \cos \theta_r + n_t \cos \theta_t} = 4\pi \frac{\omega_{sum}}{c} \frac{i}{n_i \cos \theta_r + n_t \cos \theta_t}$$

$$\text{Snell's law: } \sin \theta_t = \left(\frac{n_i}{n_t}\right) \sin \theta_i = \frac{\sin \theta_i}{n_{ti}}$$

$$L_{s,y}^r = 4\pi i \frac{\omega_{sum}}{cn_i} \left[ \frac{1}{\cos \theta_r + n_{ti} \sqrt{1 - \left(\frac{\sin \theta_i}{n_{ti}}\right)^2}} \right] = 4\pi \frac{\omega_{sum}}{cn_i} \frac{i}{\cos \theta_r + \sqrt{n_{ti}^2 - \sin^2 \theta_t}} =$$

$$= 4\pi \frac{\omega_{sum}}{cn_i} \frac{i}{\cos \theta_r + \sqrt{n_{ti}^2 - \sin^2 \theta_t}} = 4\pi \frac{\omega_{sum}}{cn_i} \frac{i}{\cos \theta_r + i \sqrt{\sin^2 \theta_t - n_{ti}^2}} = 4\pi \frac{\omega_{sum}}{cn_i} \frac{i \cos \theta_r + \sqrt{\sin^2 \theta_t - n_{ti}^2}}{\cos^2 \theta_r + \sin^2 \theta_t - n_{ti}^2} =$$

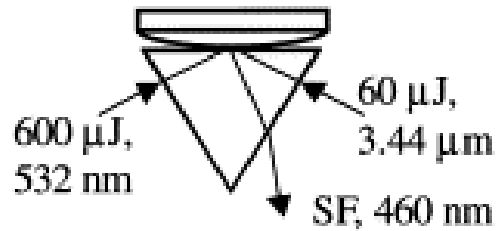
$$= 4\pi \frac{\omega_{sum}}{cn_i} \frac{i \cos \theta_r + \sqrt{\sin^2 \theta_t - n_{ti}^2}}{1 - n_{ti}^2} = 4\pi \frac{\omega_{sum}}{cn_i} \frac{(\sin^2 \theta_t - n_{ti}^2)^{1/2}}{1 - n_{ti}^2} + 4\pi \frac{\omega_{sum}}{cn_i} \frac{i \cos \theta_r}{1 - n_{ti}^2}$$



Since each Fresnel coefficient is at least a factor of 2 larger at  $\theta_c$  than at normal incidence, it is evident that TIR at the critical angle can lead to very large increases in signal.

# The TIR geometry

(a)



- plano-convex  $\text{MgF}_2$  lens
  - a diameter of 25.4 mm
  - radius of curvature of 59.9 mm
- equilateral  $\text{CaF}_2$  prism
  - dimensions of  $15 \times 15 \text{ mm}^2$



# Result

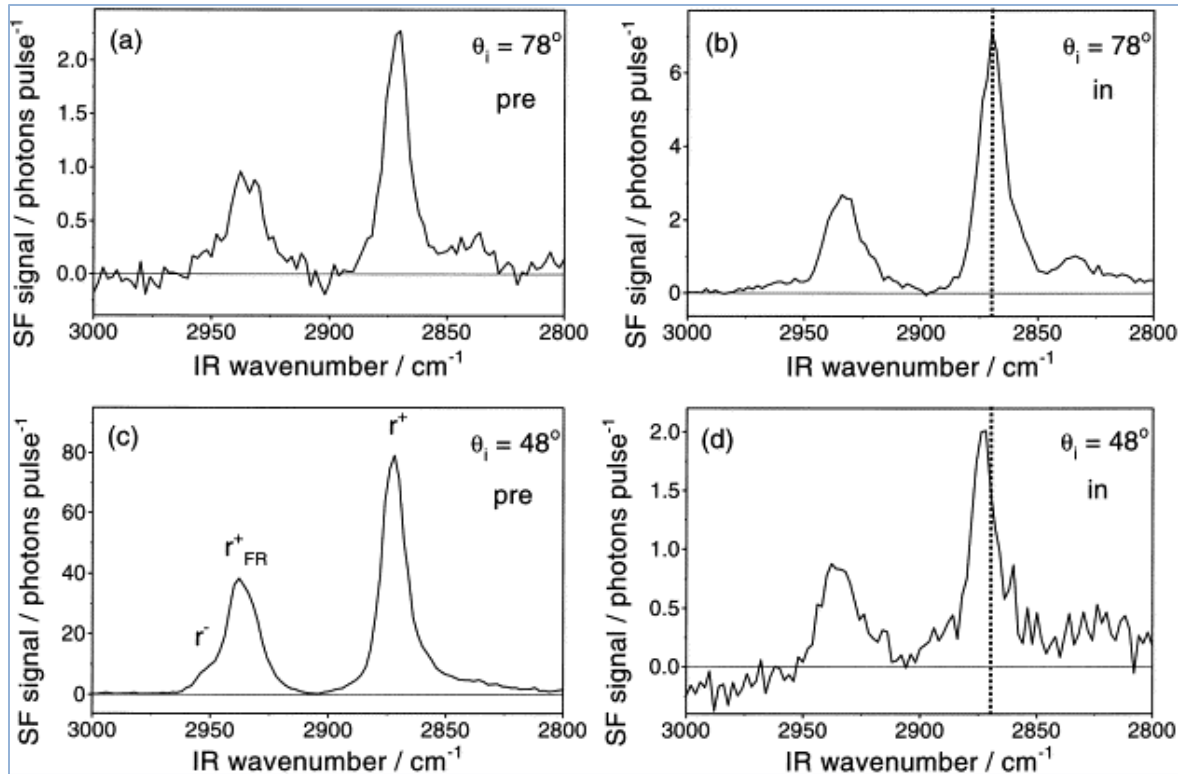


Fig. 6. TIR SF spectra of Zn arachidate at the CaF<sub>2</sub>/air and CaF<sub>2</sub>/MgF<sub>2</sub> interfaces: (a)  $\theta_i=78^\circ$ , pre-contact, (b)  $\theta_i=78^\circ$ , in-contact, (c)  $\theta_i=48^\circ$ , pre-contact, and (d)  $\theta_i=48^\circ$ , in-contact. All spectra were recorded with an acquisition time of 30 s at each data point except (c), which was recorded with an acquisition time of 5 s at each data point. Laser powers used for spectra (a) and (b) were 300  $\mu\text{J pulse}^{-1}$  at 532 nm and 40  $\mu\text{J pulse}^{-1}$  in the IR. Laser powers used for spectra (c) and (d) were 500  $\mu\text{J pulse}^{-1}$  at 532 nm and 60  $\mu\text{J pulse}^{-1}$  in the IR.

| Peak                              | 78°   | 48°   |
|-----------------------------------|-------|-------|
|                                   | Ratio | Ratio |
| SFS                               |       |       |
| $r^+(2874 \text{ cm}^{-1})$       | 3.45  | 0.023 |
| $r^+_{FR} (2936 \text{ cm}^{-1})$ | 2.78  | 0.032 |

# Summary

- TIR
- Fresnel coefficients at TIR

# The TIR geometry used for the SF

$$p_m = \frac{4Ea}{3\pi R} \Rightarrow$$

$R$  – the radius of curvature of the lens  
 $E$  – the reduced Young's modulus of the two materials

$$\frac{1}{E} = \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}$$

$\nu_i$  – the Poisson ratio

$E_i$  – the Young's modulus of material  $i$

$a$  – the radius of the contact spot

