

THE JOURNAL OF CHEMICAL PHYSICS 132, 234503 (2010)

## **Temporal effects on spectroscopic line shapes, resolution, and sensitivity of the broad-band sum frequency generation**

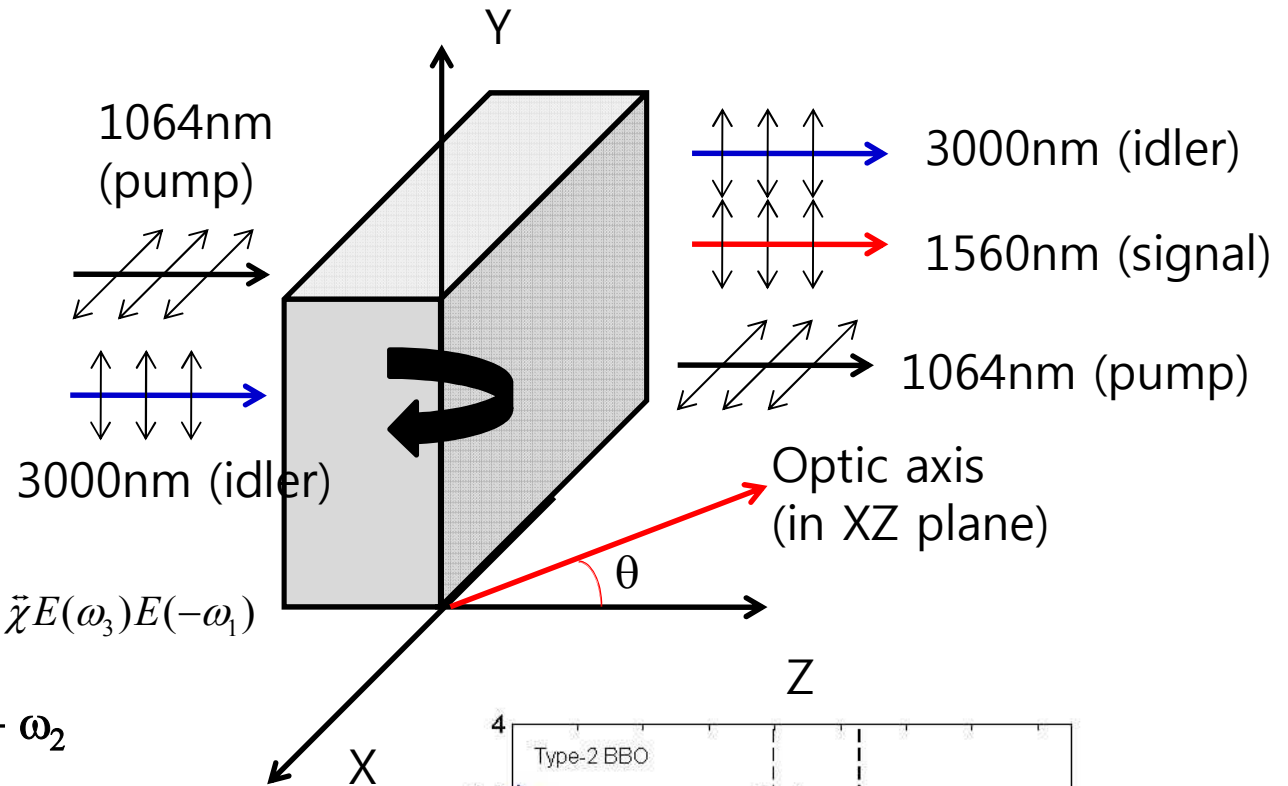
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# Conventional SFG system

## Conventional SFG system - controlling IR wavelength by Angle tuning



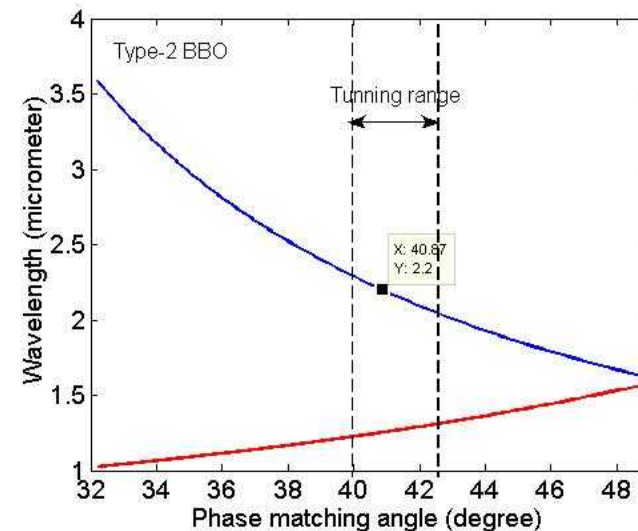
Second order process:  $P(\omega_2) = \tilde{\chi} E(\omega_3) E(-\omega_1)$

Energy conservation :  $\omega_3 = \omega_1 + \omega_2$

Momentum conservation :

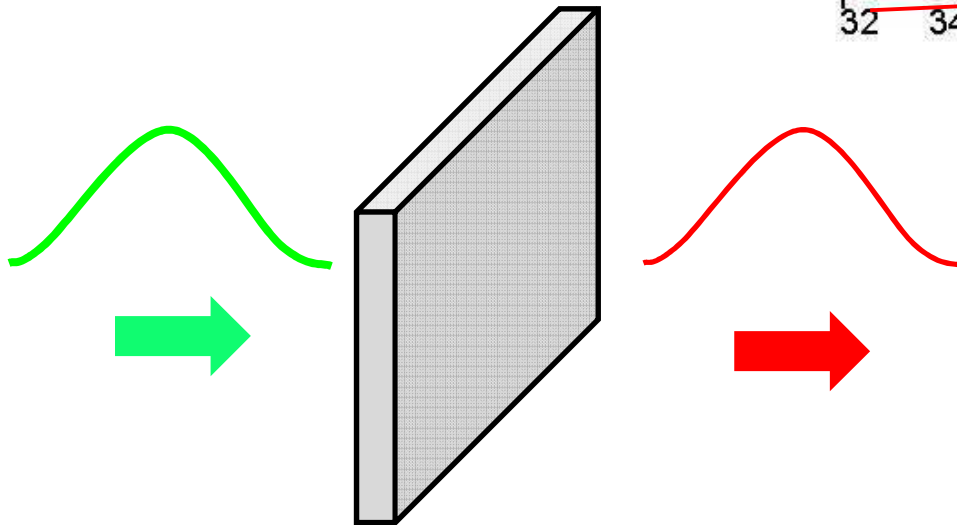
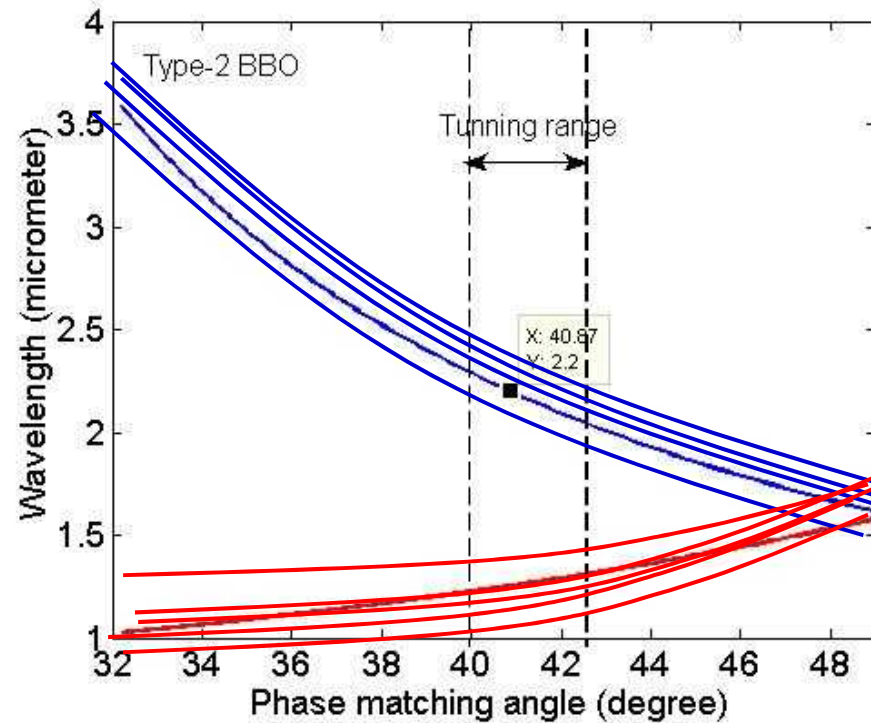
$$\mathbf{n}_{3,e} \mathbf{k}_3 = \mathbf{n}_{1,o} \mathbf{k}_1 + \mathbf{n}_{2,o} \mathbf{k}_2$$

$$\frac{1}{n_e^2(\omega_3)} = \frac{\cos^2 \theta}{n_o(\omega_3)^2} + \frac{\sin^2 \theta}{n_e'(\omega_3)^2}$$

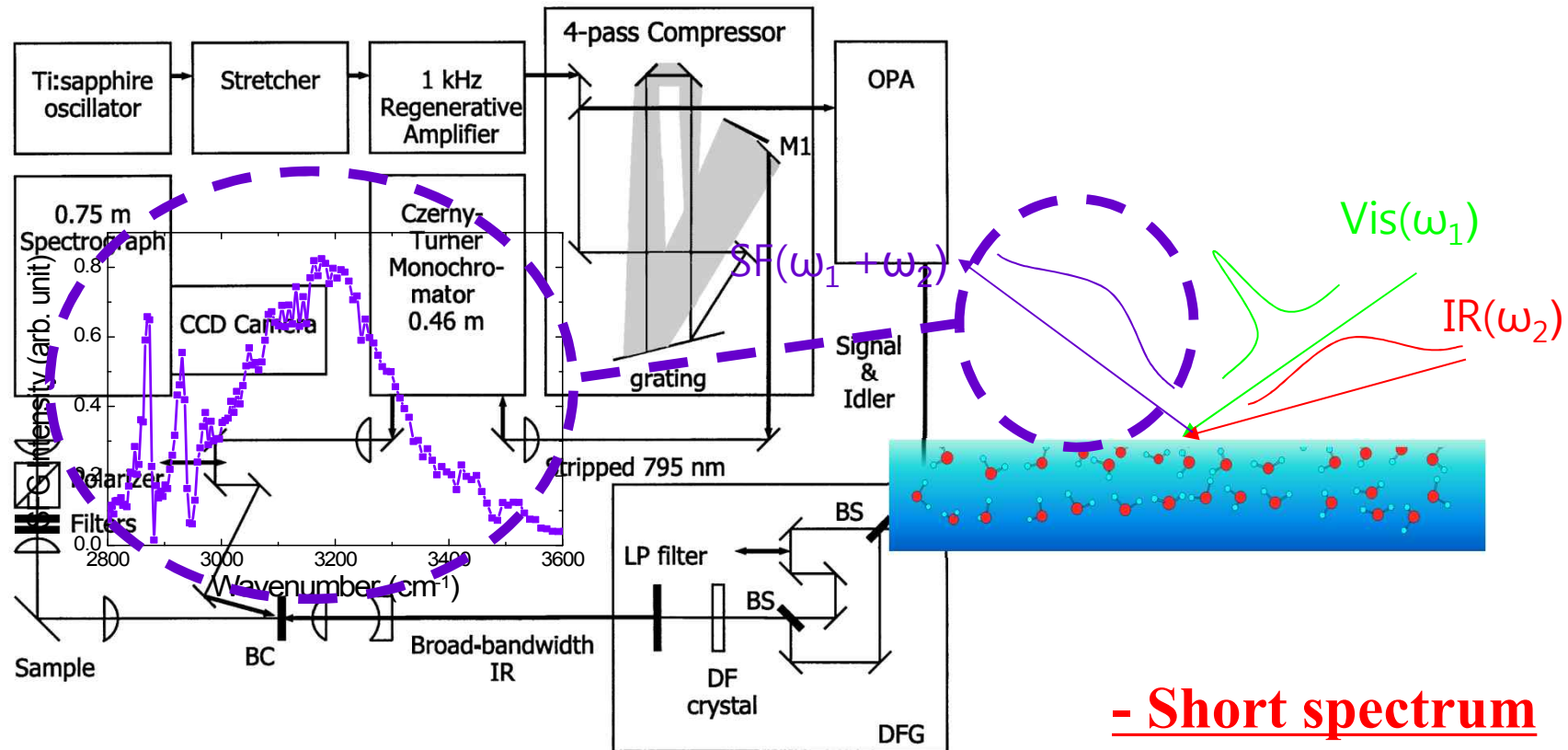


# Broadband SFG system

**Broadband SFG  
system -  
no angle tuning**



# Broadband SFG system

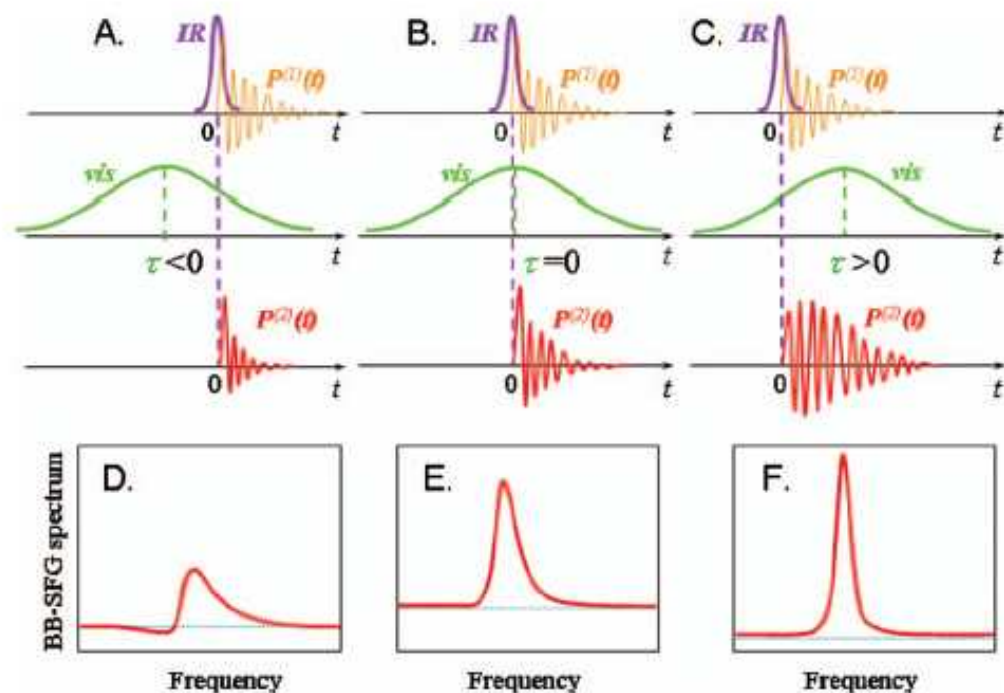


- Short spectrum acquisition time

- Sub picosecond time resolving

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# Spectral resolution of BBSFG



Molecular vibrational  
damping time 1-10ps  
(except strong damping)

Second order  
interaction can be  
truncated by visible  
pulse

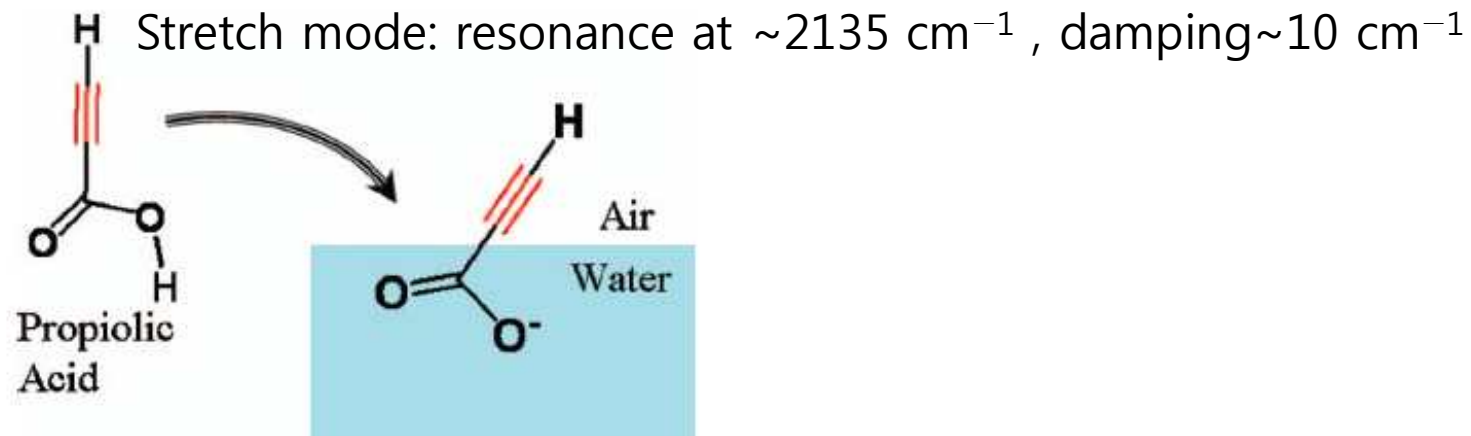


Lorenztian line shape is  
broken

$$P^{(2)}(t) = \int_{-\infty}^{+\infty} dt_1 \int_{-\infty}^{+\infty} dt_2 S^{(2)}(t_1, t_2) E(t - t_2) E(t - t_2 - t_1). \quad (1)$$

# Spectral resolution of BBSFG

- Q: 1) What time delay makes SFG spectra better??**  
**2) How about visible pulse shape??**



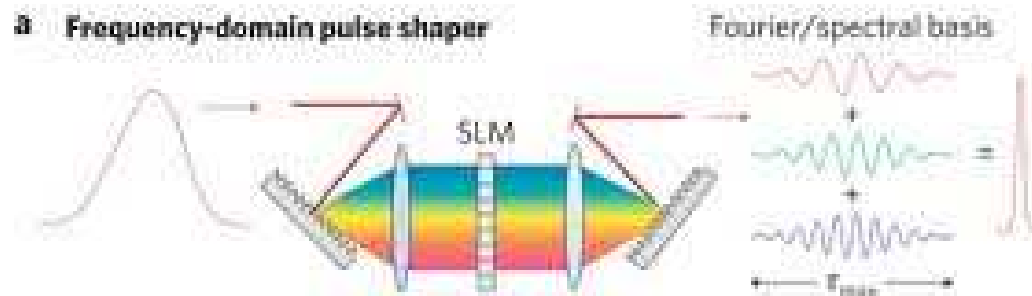
SCHEME 1.

**Take SFG spectra of Air / water interface with varying time delay  
(-1000fs  $\sim$  +1000fs)**

# Preparation for experiment

## 1) 4f pulse shaper

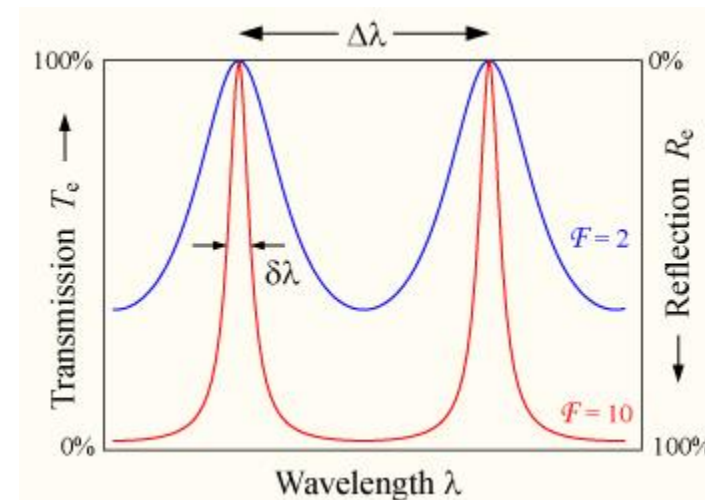
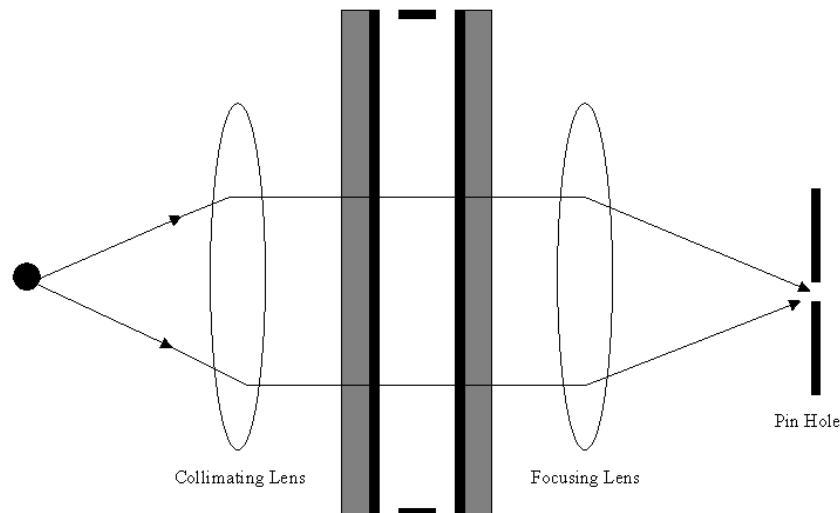
a Frequency-domain pulse shaper



$$E_{\text{vis}}^{\text{stretcher}}(t) = \frac{1}{2} E_{\text{vis}}^0 \int_{\omega_{\text{vis}} - \sigma}^{\omega_{\text{vis}} + \sigma} \exp(-i\omega t) d\omega$$

$$= E_{\text{vis}}^0 \frac{\sin(\sigma t)}{t} \exp(-i\omega_{\text{vis}} t),$$

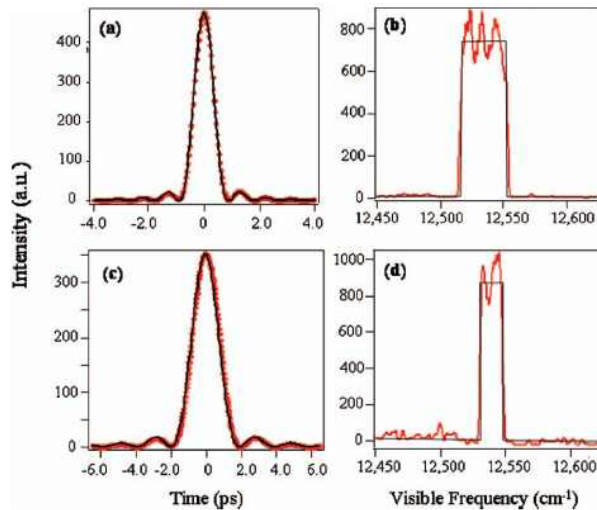
## 2) Fabry–Perot etalon





# Preparation for experiment

## 1) 4f pulse shaper



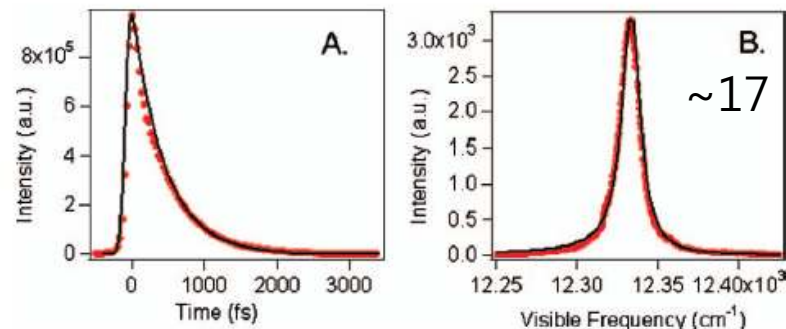
$\sim 37 \text{ cm}^{-1}$

$\sim 17 \text{ cm}^{-1}$

$$E_{\text{vis}}^{\text{stretcher}}(t) = \frac{1}{2} E_{\text{vis}}^0 \int_{\omega_{\text{vis}} - \sigma}^{\omega_{\text{vis}} + \sigma} \exp(-i\omega t) d\omega$$

$$= E_{\text{vis}}^0 \frac{\sin(\sigma t)}{t} \exp(-i\omega_{\text{vis}} t),$$

## 2) Fabry–Perot etalon



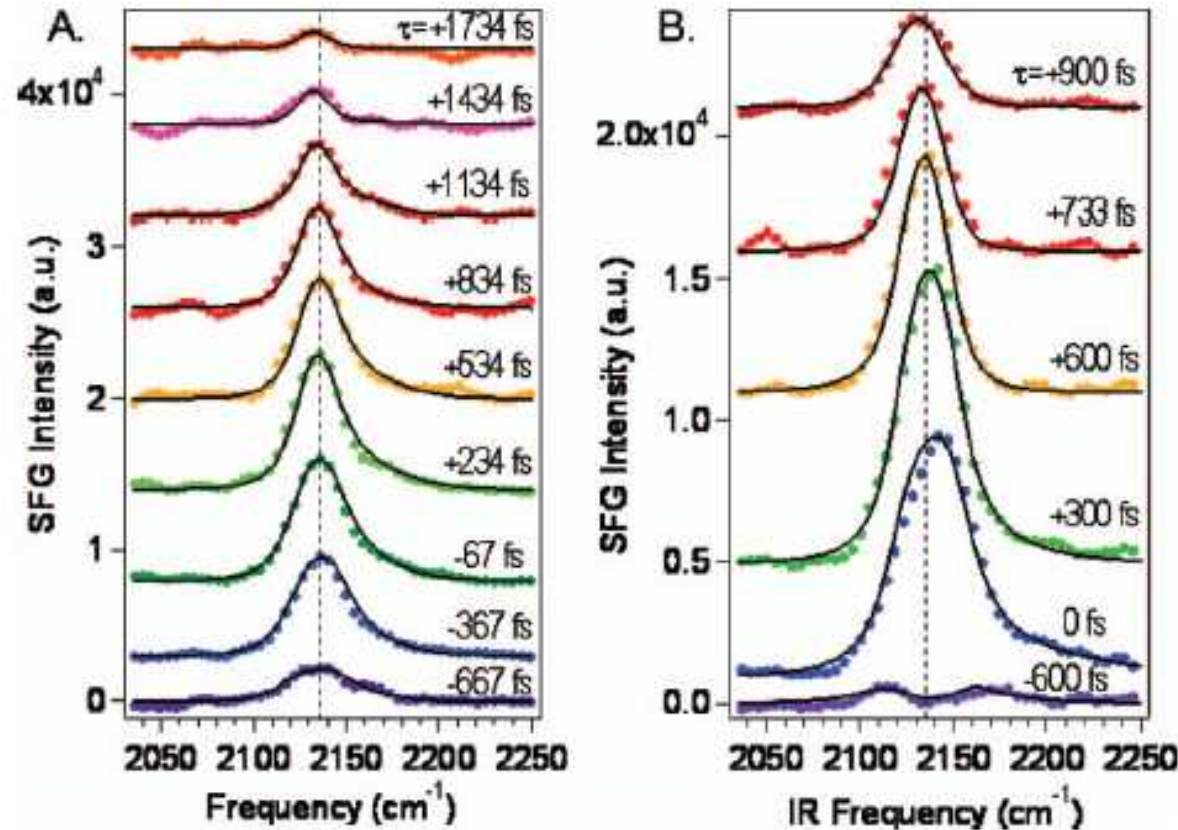
$\sim 17 \text{ cm}^{-1}$

$$E_{\text{vis}}^{\text{etalon}}(t) = E_{\text{vis}}^0 (1 - R) \sum_{n=0}^{\infty} R^n \exp\left\{-\frac{(t - n\tau_{\text{RT}})^2}{\tau_{\text{vis}}^2}\right\}$$

$$\times \exp\{-i\omega_{\text{vis}}(t - n\tau_{\text{RT}})\}.$$



# SFG spectra with 4f pulse shaper



➡ At positive time delay ( $t_2 > t_1$ ) spectrum looks more similar to Lorentzian line shape

# SFG spectra with 4f pulse shaper - fitting

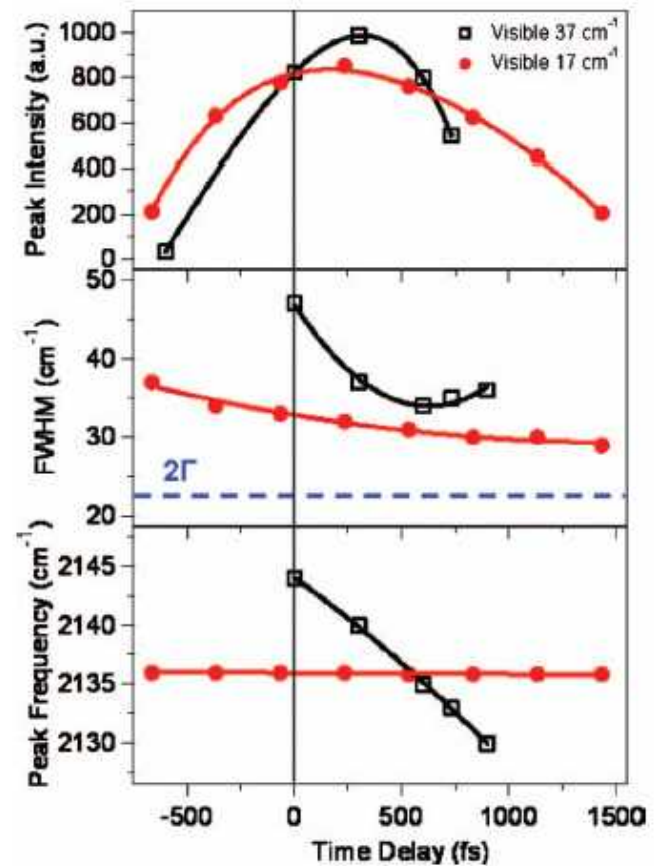
$$P^{(2)}(t) = \int_{-\infty}^{+\infty} dt_1 \int_{-\infty}^{+\infty} dt_2 S^{(2)}(t_1, t_2) E(t - t_2) E(t - t_2 - t_1).$$

$$S(t_1) = A_{\text{NR}} \exp(i\varphi_{\text{NR}}) \delta(t_1) - i\theta(t_1) B \Gamma \exp(-i\omega_0 t_1 - \Gamma t_1).$$

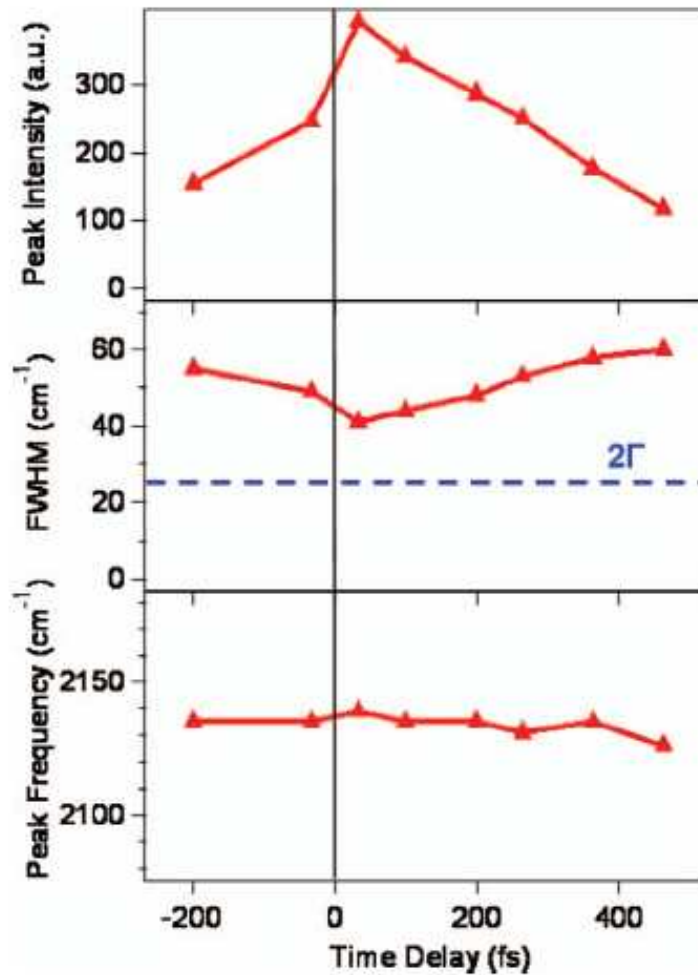
$$E_{\text{IR}}(t) = \sum_j E_{\text{IR}j}^0 \exp\left\{-\frac{(t-t_j)^2}{\tau_{\text{IR}j}^2}\right\} \exp(-i\omega_{\text{IR}j}t).$$

$$E_{\text{vis}}^{\text{stretcher}}(t) = \frac{1}{2} E_{\text{vis}}^0 \int_{\omega_{\text{vis}} - \sigma}^{\omega_{\text{vis}} + \sigma} \exp(-i\omega t) d\omega$$

$$= E_{\text{vis}}^0 \frac{\sin(\sigma t)}{t} \exp(-i\omega_{\text{vis}} t),$$



# SFG spectra with etalon- fitting



Sharp change near zero delay  
: due to steep edge of visible pulse