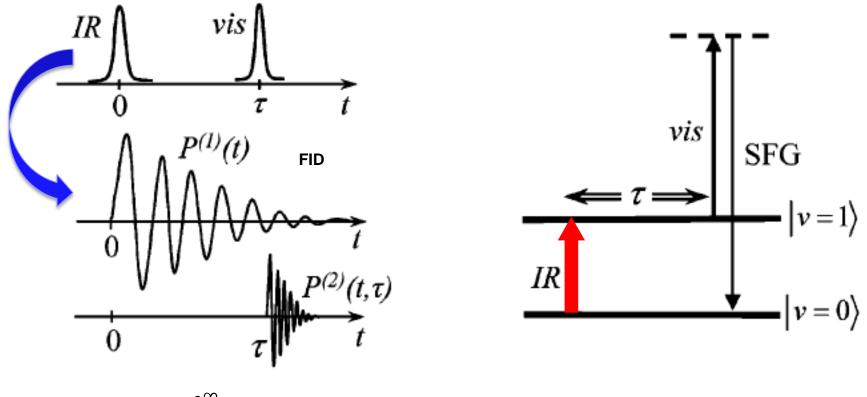
# Time-Domain Description of the SFG Spectroscopy

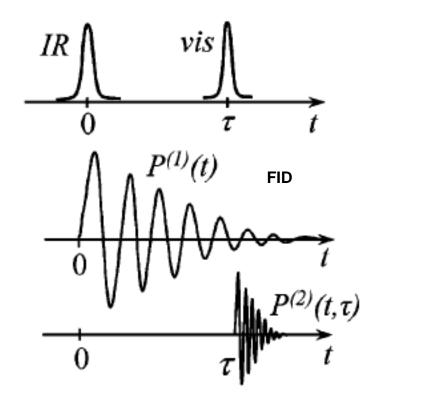
Journal Club 2015.10.02 Zaure The excitation of an ensemble of molecules by fs IR pulse which creates a transient first-order polarization  $P^{(1)}(t)$ .

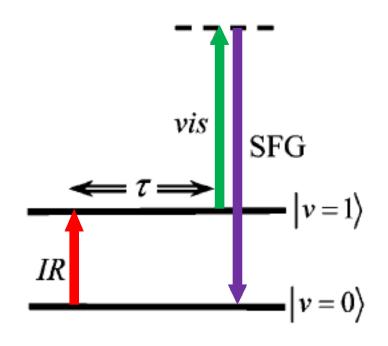


$$P^{(1)}(t) = \int_0^\infty dt_1 R(t_1) E_{IR}(t - t_1) = R(t) \otimes E_{IR}(t)$$

*R*-molecular response function

This  $P^{(1)}(t)$  via optical upconversion with the overlapping VIS pulse (non-resonant) gives rise to  $P^{(2)}(t)$ , oscillating at a frequency that is the sum of the infrared and the visible frequencies.





 $P^{(2)}(t;\tau) \propto E_{SFG}(t;\tau)$ 

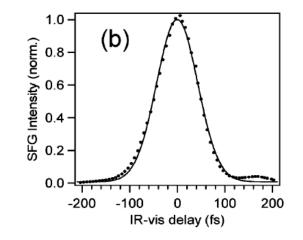
$$E_{SFG}(t;\tau) = \int_0^\infty dt_2 \int_0^\infty dt_1 R^{(2)}(t_2,t_1;\tau) E_{vis}(t-t_2) E_{IR}(t-t_2-t_1)$$

 $\square R^{(2)}(t_1, t_2) \approx R(t_1)\delta(t_2)$  (approximation)

$$\square P^{(1)}(t) = \int_0^\infty dt_1 R(t_1) E_{IR}(t - t_1) = R(t) \otimes E_{IR}(t) \text{ (convolution)}$$

$$E_{SFG}(t;\tau) = E_{vis}(t;\tau) \int_0^\infty dt_1 R(t_1) E_{IR}(t-t_1) = [R(t) \otimes E_{IR}(t)] E_{vis}(t;\tau)$$

$$I_{SFG-FID}(\tau) \propto \int_{-\infty}^{+\infty} |E_{SFG}(t,\tau)|^2 dt$$



Fourier transformation:

$$E_{SFG}(t,\tau) \implies \tilde{E}_{SFG}(\omega,\tau)$$

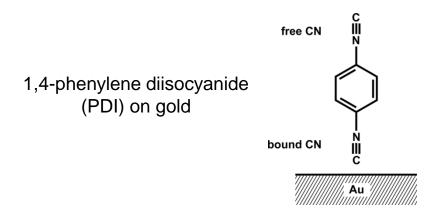
$$\tilde{E}_{SFG}(\omega,\tau) \propto \int_{-\infty}^{+\infty} E_{SFG}(t,\tau) e^{i\omega t} dt = \int_{-\infty}^{+\infty} [R(t) \otimes E_{IR}(t)] E_{vis}(t,\tau) e^{i\omega t} dt$$
$$= [\tilde{R}(\omega)\tilde{E}_{IR}(\omega)] \otimes \tilde{E}_{vis}(\omega,\tau)$$

 $I_{SFG}(\omega,\tau) \propto \left| \tilde{E}_{SFG}(\omega,\tau) \right|^2$ 

Time-Domain SFG Spectroscopy Using Mid-IR Pulse Shaping: Practical and Intrinsic Advantages

Jennifer E. Laaser, Wei Xiong, and Martin T. Zanni J. Phys. Chem. B 2011, 115, 2536–2546

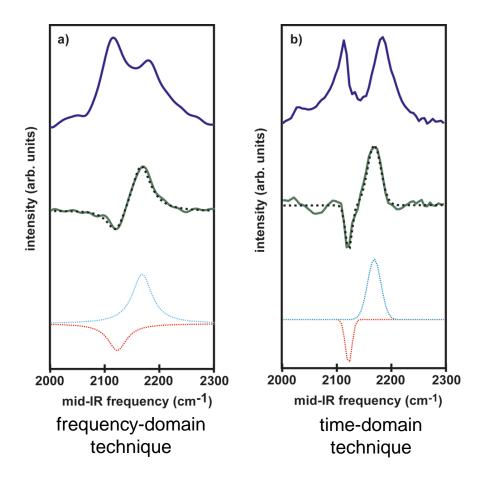
#### PDI Monolayer on Gold



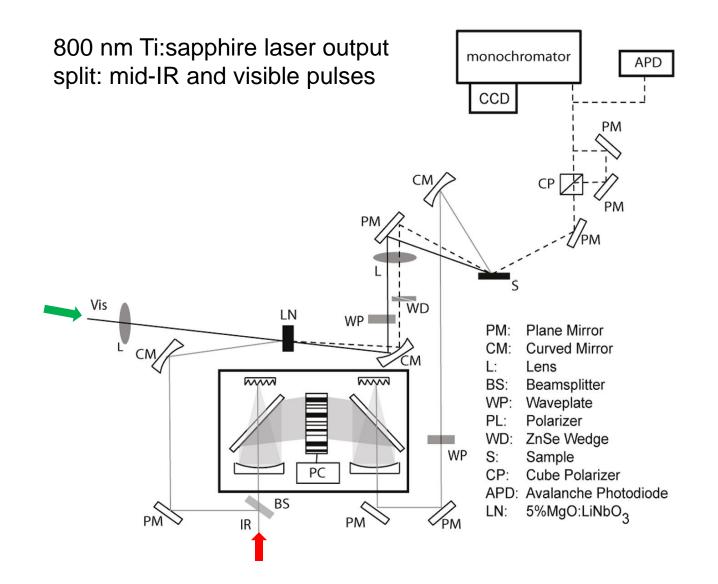
The conjugated ring structure facilitates electron transfer, the two CN groups allow contact with two metal electrodes, and the electronic coupling to the metal is stronger than for comparable thiol compounds, providing a lower barrier to electron transport. One important property of PDI is the structural heterogeneity with which it binds to the metal surface, because the binding mode will influence the electronic coupling strength between the molecular electronic orbitals and the metal surface.

# Time-domain approach for SFG spectroscopy produces spectra that are much more accurate

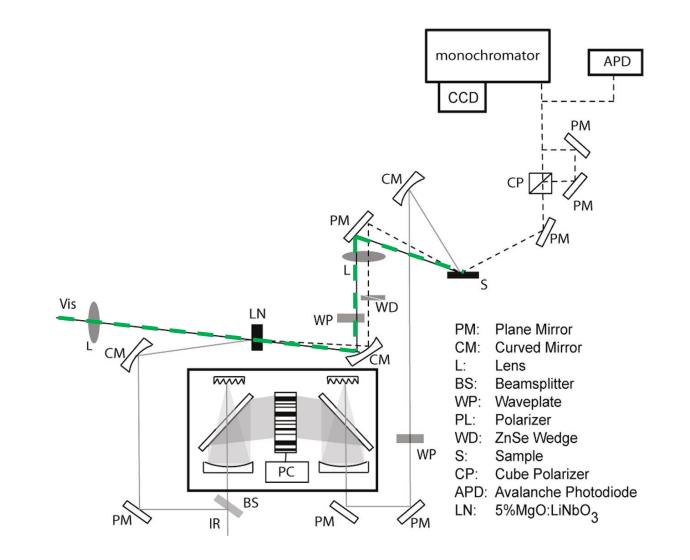
Shaper-based Phase-stable Heterodyned SFG



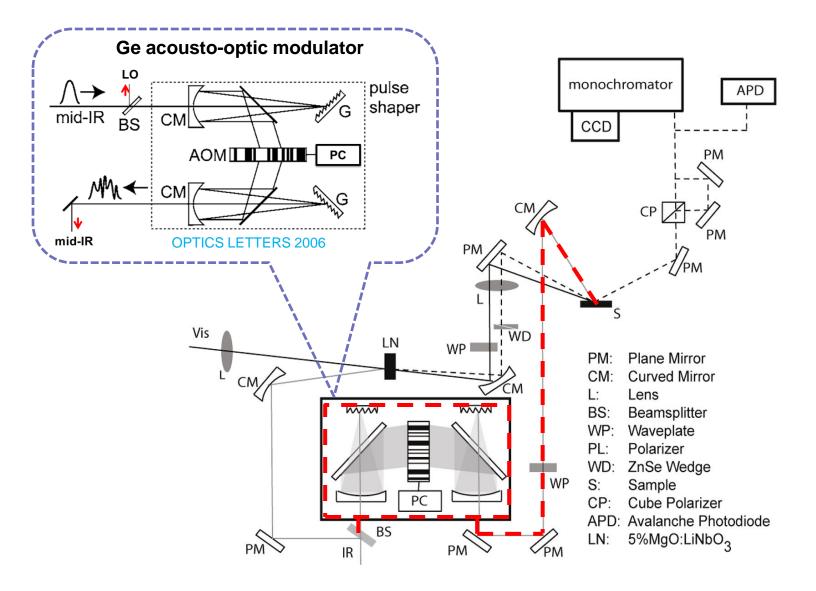
Shaper-based Phase-stable Heterodyned SFG



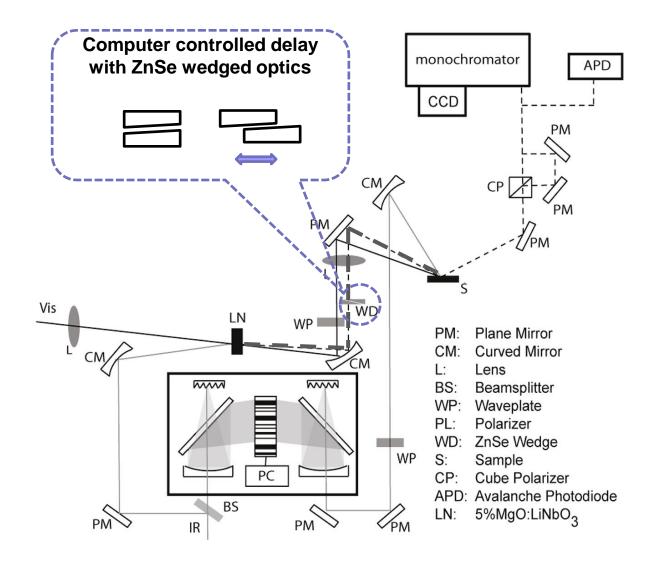
## Visible Beam



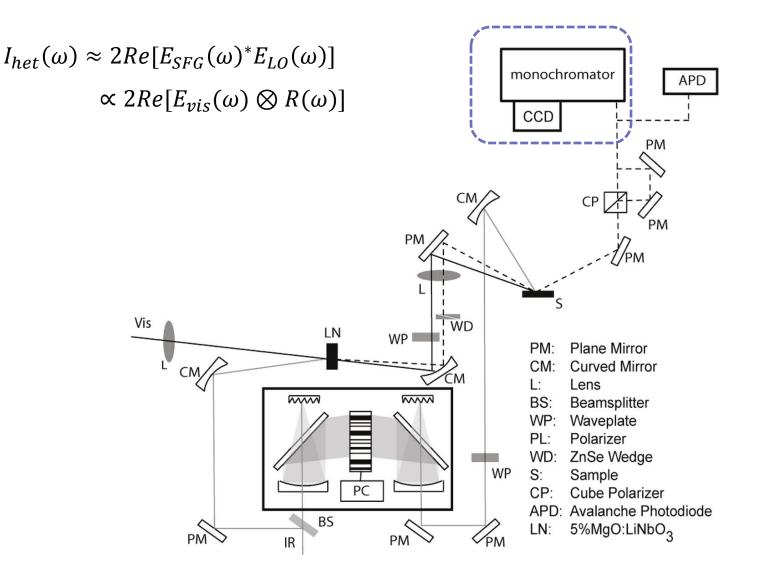
## mid-IR

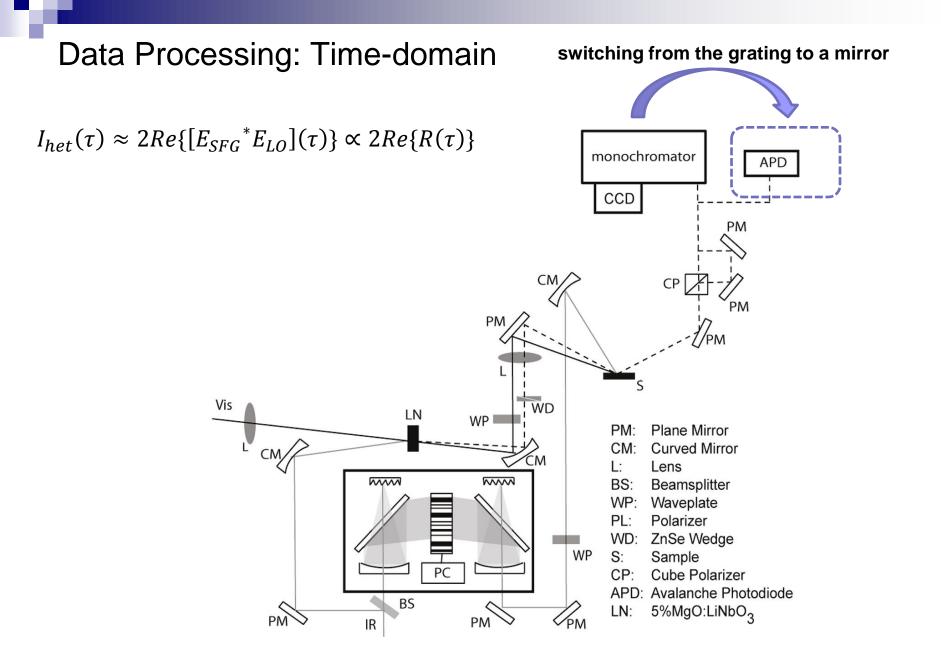


#### Local Oscillator Generation



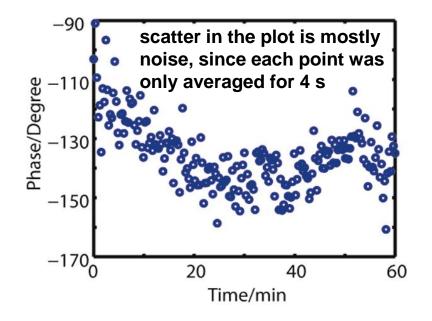
Data Processing: Frequency-domain





#### Phase Stability

- LO and vis pulses follow nearly the same path btw the LiNbO<sub>3</sub> (LN) crystal and the sample.
- LO through ZnSe wedges provides highly accurate time delays and no phase drift!
- Phase drift of only 1.5°/min, so scans can be averaged for several minutes.
- Stability is about 6 times better!

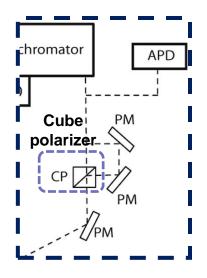


#### Balanced HD SFG signals in the frequency domain

Ex: if a 50/50 beam splitter is used to combine LO and emitted field at a 90° angle, then the two measured signals

$$\begin{aligned} & \text{Subtract} \\ |E_{LO} + E^{(2)}|^2 &= |E_{LO}|^2 + 2Re(E_{LO}^*E^{(2)}) + |E^{(2)}|^2 \\ |E_{LO} - E^{(2)}|^2 &= |E_{LO}|^2 - 2Re(E_{LO}^*E^{(2)}) + |E^{(2)}|^2 \end{aligned}$$

- Here, LO polarisation ⊥ to the desired signal and insert a CP after the sample oriented at 45° relative to the local oscillator and signal polarizations.
- So, LO and signal fields are projected onto two orthogonal polarization axes, which necessitates that their interference is 180° out-of-phase, as in eqs.

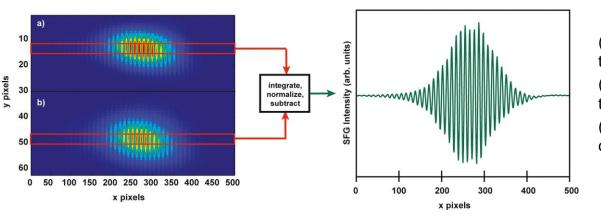


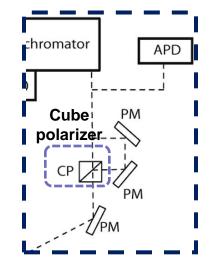
#### Balanced HD SFG signals in the frequency domain

Ex: if a 50/50 beam splitter is used to combine LO and emitted field at a 90° angle, then the two measured signals.

$$\begin{aligned} \left| E_{LO} + E^{(2)} \right|^2 &= |E_{LO}|^2 + 2Re(E_{LO}^*E^{(2)}) + |E^{(2)}|^2 \\ \left| E_{LO} - E^{(2)} \right|^2 &= |E_{LO}|^2 - 2Re(E_{LO}^*E^{(2)}) + |E^{(2)}|^2 \end{aligned}$$

- Here, LO polarisation ⊥ to the desired signal and insert a CP after the sample oriented at 45° relative to the local oscillator and signal polarizations.
- As a result, LO and signal fields are projected onto two orthogonal polarization axes, which necessitates that their interference is 180° out-of-phase, as in eqs.





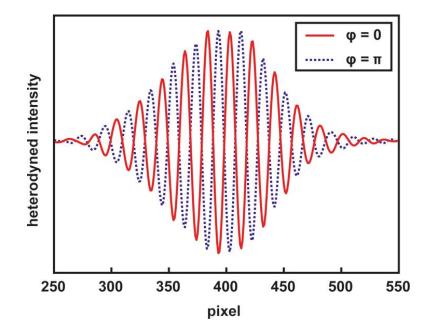
(a) Image of the interference pattern from beam transmitted through the polarizer,

(b) interference pattern from beam rejected by the polarizer,

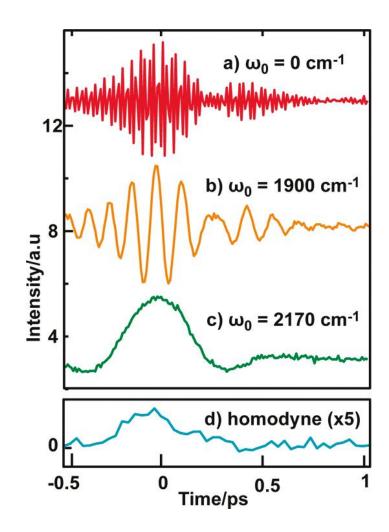
(c) subtracted trace illustrating background cancellation

# Phase Control with Mid-IR Pulse Shaping

Frequency-domain heterodyned signals obtained with phases of 0 (red, solid) and  $\pi$  (blue, dotted) applied to the IR pump pulse using the pulse shaper.



#### Time Domain in the Rotating Frame



## **Measurements Results**

