

Chemical Bonding I

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H.Haken & H.C.Wolf, Molecular Physics and Elements of Quantum Chemistry
P.Atkins & R.Friedman, Molecular Quantum Mechanics

Proceedings of the National Academy of Sciences
Vol. 65, No. 4, pp. 823–830, April 1970

Failure of Energy Transfer between Identical Aromatic Molecules on Excitation at the Long Wave Edge of the Absorption Spectrum

Gregorio Weber and Meir Shinitzky

DEPARTMENT OF CHEMISTRY AND CHEMICAL ENGINEERING, UNIVERSITY OF ILLINOIS, URBANA

Proceedings of the National Academy of Sciences
Vol. 67, No. 3, pp. 1116–1121, November 1970

Role of Heterogeneity of the Solvation Site in Electronic Spectra in Solution*

William C. Galley and Robert M. Purkey

DEPARTMENT OF CHEMISTRY, MCGILL UNIVERSITY, MONTREAL, CANADA

Communicated by Norman Davidson, August 3, 1970

Chemical Bonding

Heteropolar Bonding (Ionic Bonding)

Example : $\text{Na}^+ \text{Cl}^-$

Homopolar Bonding (Covalent Bonding, After Quantum Mechanics)

Example : H^2

How could a hydrogen molecule be formed from two **neutral H atoms?**

The Hydrogen Molecule-Ion, H_2^+

The simplest case of chemical bonding

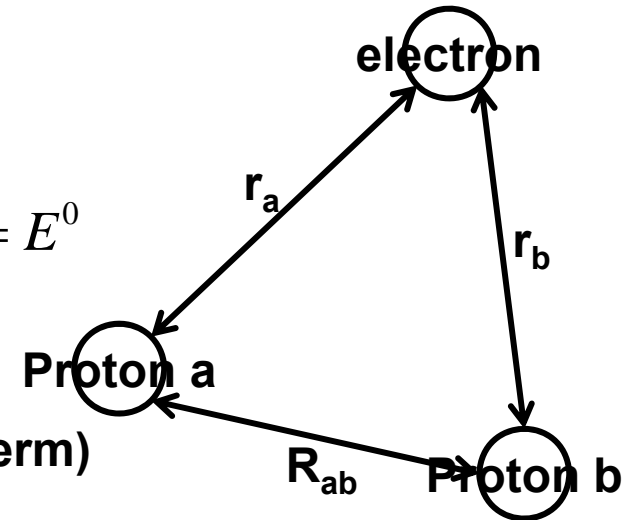
Starting from Hydrogen atom

$$\left(-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_a}\right)\phi_a(r_a) = E_a^0\phi_a(r_a) \quad E_a^0 = E_b^0 = E^0$$

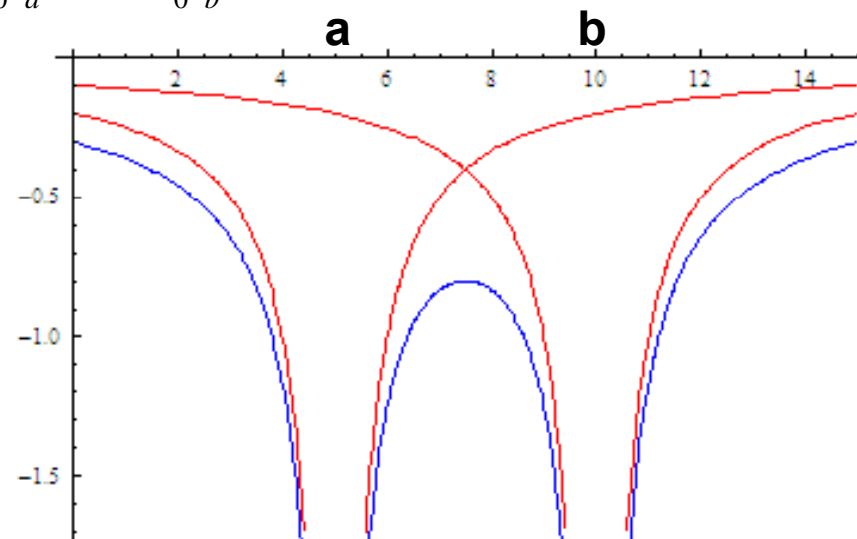
Adding a second proton

(Later, I consider electron interaction term)

$$\left(-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_a} - \frac{e^2}{4\pi\epsilon_0 r_b}\right)\psi = E\psi$$



Potential Curve



Red : each wave fn.
Blue : added wave fn.

The Hydrogen Molecule-Ion, H_2^+

Determinating the wavefunction ψ

Assume wavefunction $\psi = c_1\phi_a + c_2\phi_b$

$$\left(\underbrace{-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_a} - \frac{e^2}{4\pi\epsilon_0 r_b}}_{E^0} \right) c_1\phi_a + \left(\underbrace{-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_b} - \frac{e^2}{4\pi\epsilon_0 r_a}}_{E^0} \right) c_2\phi_b = E(c_1\phi_a + c_2\phi_b)$$

$$\left(\Delta E - \frac{e^2}{4\pi\epsilon_0 r_b} \right) c_1\phi_a + \left(\Delta E - \frac{e^2}{4\pi\epsilon_0 r_a} \right) c_2\phi_b = 0 \quad E^0 - E = \Delta E$$

$$\int dV (\phi_a (\Delta E - \frac{e^2}{4\pi\epsilon_0 r_b}) c_1\phi_a + \phi_a (\Delta E - \frac{e^2}{4\pi\epsilon_0 r_a}) c_2\phi_b) = 0$$

$$\int dV (\underbrace{\phi_a\phi_a}_{\equiv C} \Delta E - \underbrace{\phi_a}_{\equiv S} \frac{e^2}{4\pi\epsilon_0 r_b} \underbrace{\phi_a}_{\equiv D}) c_1 + (\underbrace{\phi_a\phi_b}_{\equiv S} \Delta E - \underbrace{\phi_a}_{\equiv D} \frac{e^2}{4\pi\epsilon_0 r_a} \underbrace{\phi_b}_{\equiv D}) c_2 = 0$$

$$(\Delta E + C)c_1 + (\Delta ES + D)c_2 = 0$$

The Hydrogen Molecule-Ion, H_2^+

$$\psi = c_1\phi_a + c_2\phi_b$$

$$\left(-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_a} - \frac{e^2}{4\pi\epsilon_0 r_b}\right)c_1\phi_a + \left(-\frac{\hbar^2}{2m_0}\nabla^2 - \frac{e^2}{4\pi\epsilon_0 r_b} - \frac{e^2}{4\pi\epsilon_0 r_a}\right)c_2\phi_b = E(c_1\phi_a + c_2\phi_b)$$

$\underbrace{\hspace{10em}}_{E^0}$
 $\underbrace{\hspace{10em}}_{E^0}$

$$\left(\Delta E - \frac{e^2}{4\pi\epsilon_0 r_b}\right)c_1\phi_a + \left(\Delta E - \frac{e^2}{4\pi\epsilon_0 r_a}\right)c_2\phi_b = 0 \qquad E^0 - E = \Delta E$$

$$\int dV (\phi_a (\Delta E - \frac{e^2}{4\pi\epsilon_0 r_b})c_1\phi_a + \phi_a (\Delta E - \frac{e^2}{4\pi\epsilon_0 r_a})c_2\phi_b) = 0$$

$$\int dV (\underbrace{\phi_a\phi_a}_{\equiv C}\Delta E - \underbrace{\phi_a}_{\equiv S}\frac{e^2}{4\pi\epsilon_0 r_b}\underbrace{\phi_a}_{\equiv D})c_1 + (\underbrace{\phi_a\phi_b}_{\equiv S}\Delta E - \underbrace{\phi_a}_{\equiv D}\frac{e^2}{4\pi\epsilon_0 r_a}\underbrace{\phi_b}_{\equiv D})c_2 = 0$$

$$(\Delta E + C)c_1 + (\Delta ES + D)c_2 = 0$$

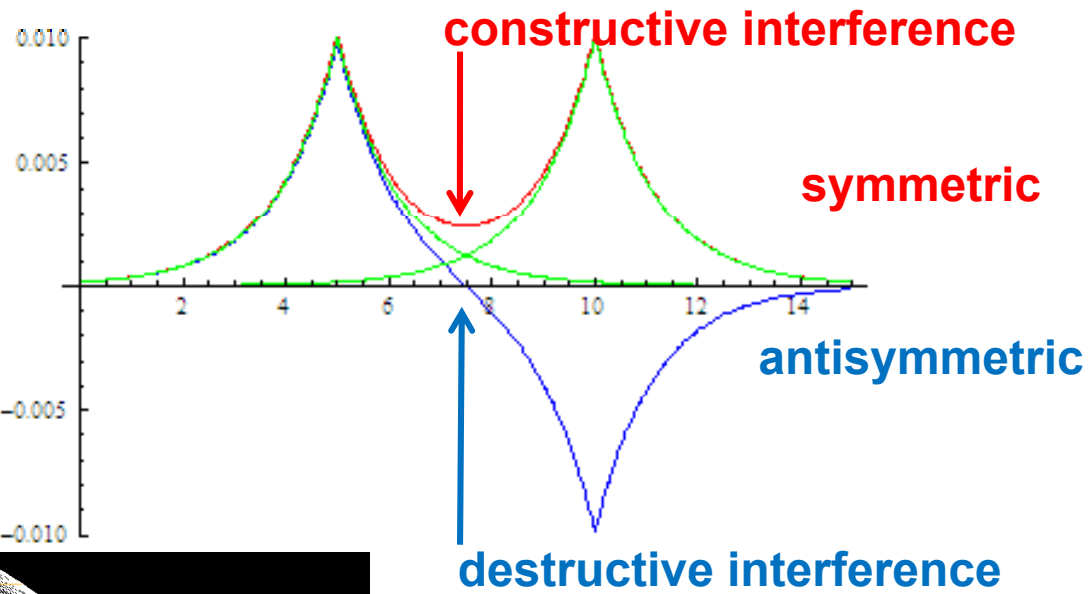
$$(\Delta ES + D)c_1 + (\Delta E + C)c_2 = 0$$

The Hydrogen Molecule-Ion, H_2^+

$$\psi = c_1\phi_a + c_2\phi_b$$

$$c_2 = -c_1 \equiv -c$$

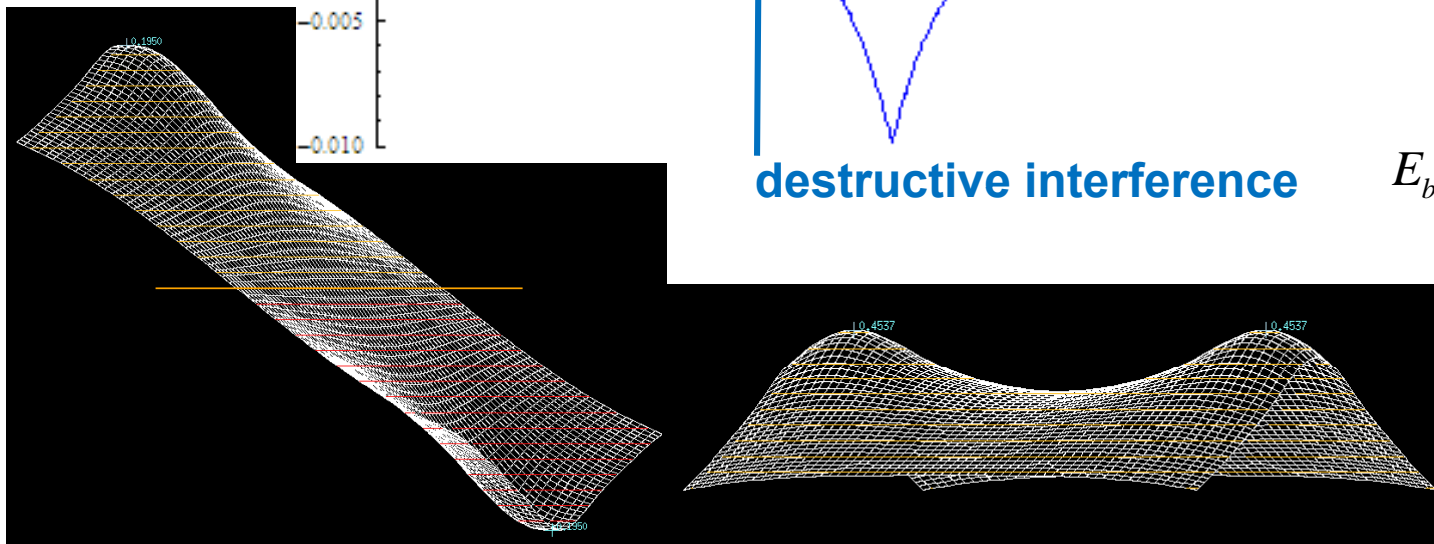
$$c_2 = c_1 \equiv c$$



$$E = E^0 + \frac{C - D}{1 - S}$$

$$E = E^0 + \frac{C + D}{1 + S}$$

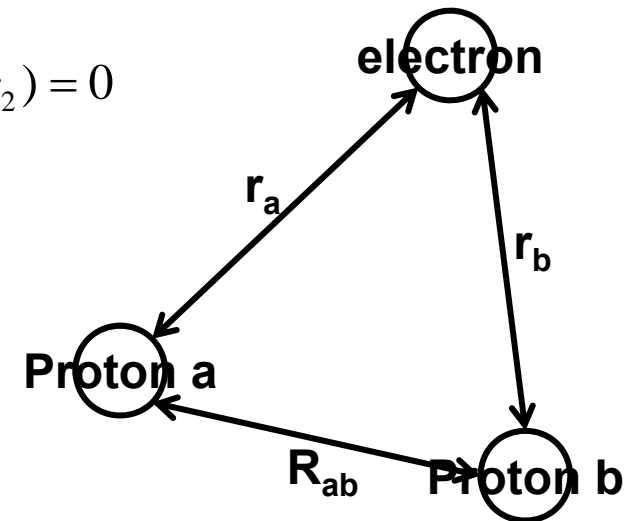
$$E_{binding} = \frac{C \pm D}{1 \pm S} + \frac{e^2}{4\pi\epsilon_0 R_{ab}}$$



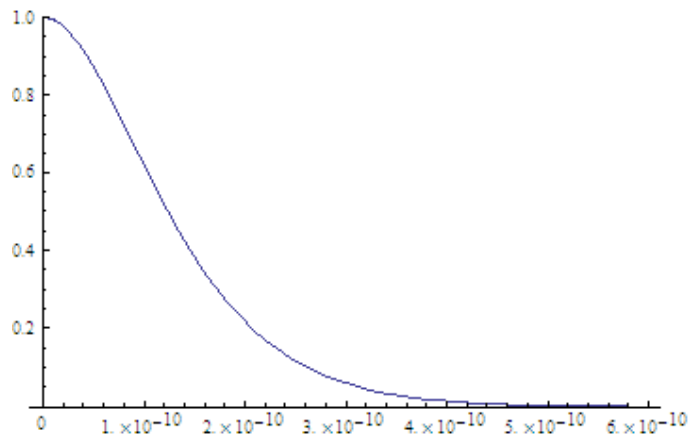
The Hydrogen Molecule-Ion, H₂⁺

$$\int dV \left(\underbrace{\phi_a \phi_a \Delta E}_{\equiv C} - \underbrace{\phi_a \frac{e^2}{4\pi\epsilon_0 r_b} \phi_a}_{\equiv S} \right) c_1 + \left(\underbrace{\phi_a \phi_b \Delta E}_{\equiv D} - \underbrace{\phi_a \frac{e^2}{4\pi\epsilon_0 r_a} \phi_b}_{\equiv D} \right) c_2 = 0$$

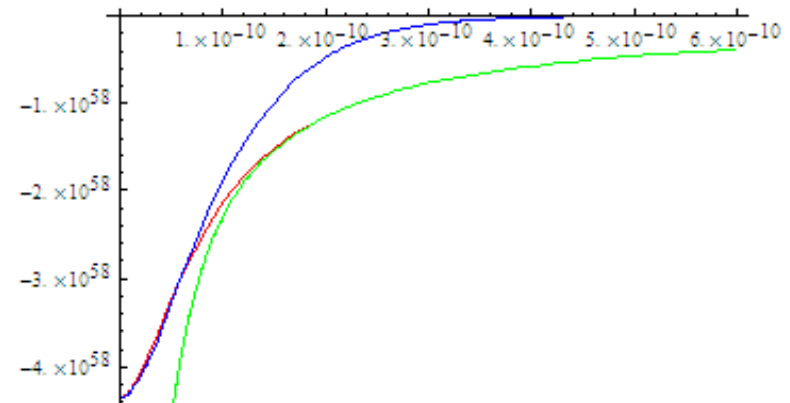
$$E_{binding} = \frac{C \pm D}{1 \pm S} + \frac{e^2}{4\pi\epsilon_0 R_{ab}}$$



For Ground State (1s state)



S : overlap integral

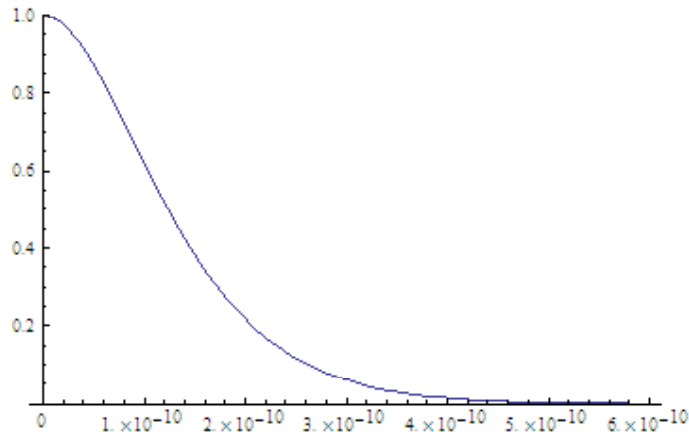


C : Coulomb integral
D: Resonance integral
(-) Proton Coulomb interaction

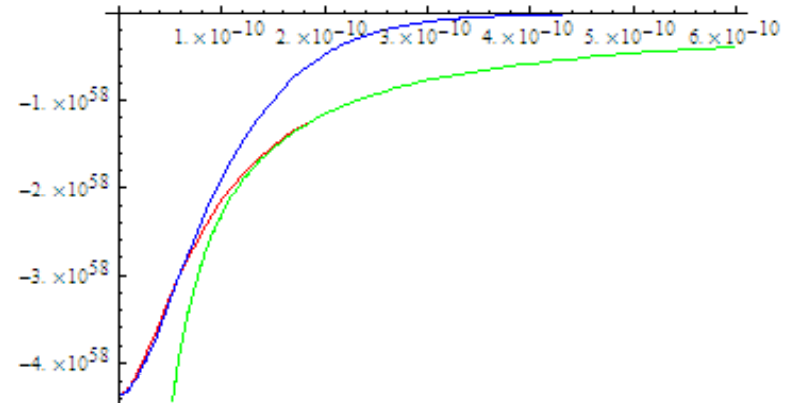
The Hydrogen Molecule-Ion, H_2^+

For Ground State (1s state)

$$E_{binding} = \frac{C \pm D}{1 \pm S} + \frac{e^2}{4\pi\epsilon_0 R_{ab}}$$



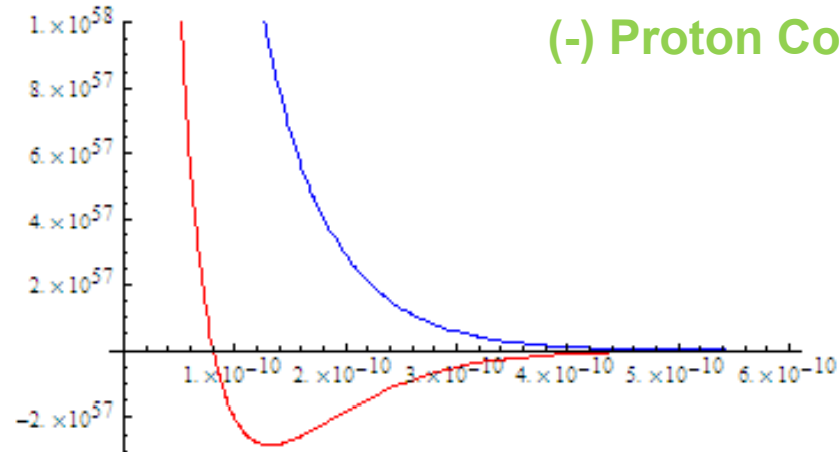
S : overlap integral



C : Coulomb integral

D: Resonance integral

(-) Proton Coulomb interaction



Bonding State (Symmetric wavefn)

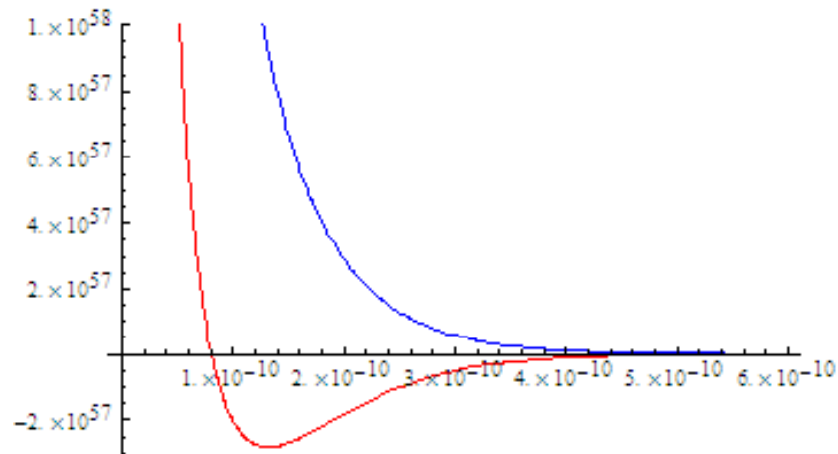
Antibonding State (Antisymmetric wavefn)

The Hydrogen Molecule-Ion, H₂⁺

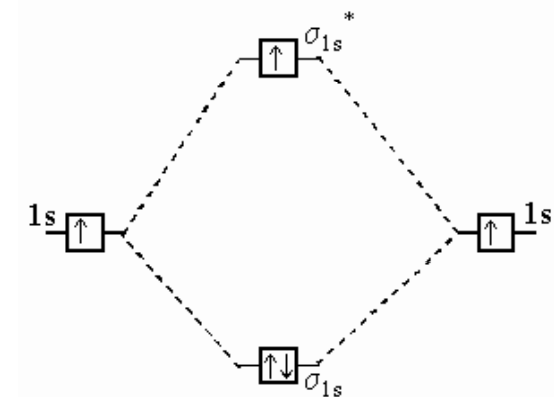
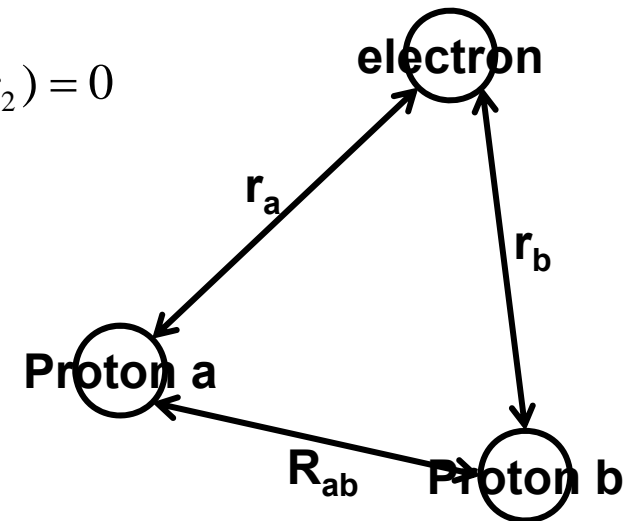
$$\int dV \left(\underbrace{\phi_a \phi_a \Delta E}_{\equiv C} - \underbrace{\phi_a \frac{e^2}{4\pi\epsilon_0 r_b} \phi_a}_{\equiv S} c_1 + \underbrace{(\phi_a \phi_b \Delta E - \phi_a \frac{e^2}{4\pi\epsilon_0 r_a} \phi_b)}_{\equiv D} c_2 \right) = 0$$

$$E_{\text{binding}} = \frac{C \pm D}{1 \pm S} + \frac{e^2}{4\pi\epsilon_0 R_{ab}}$$

For Ground State (1s state)

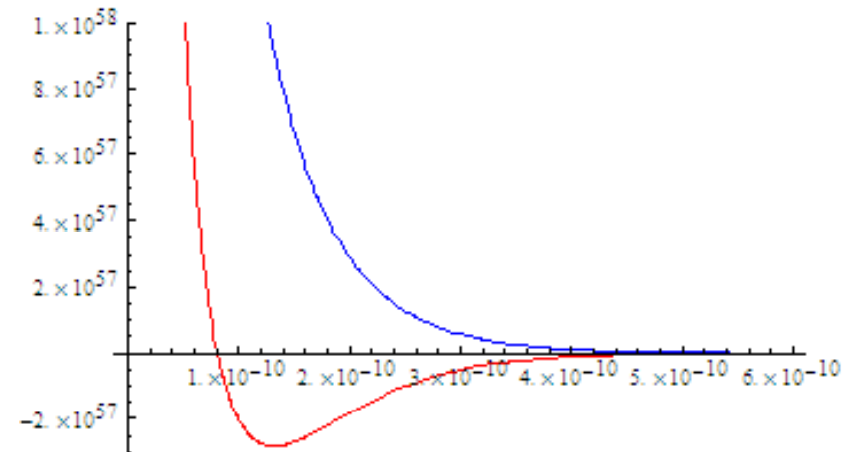
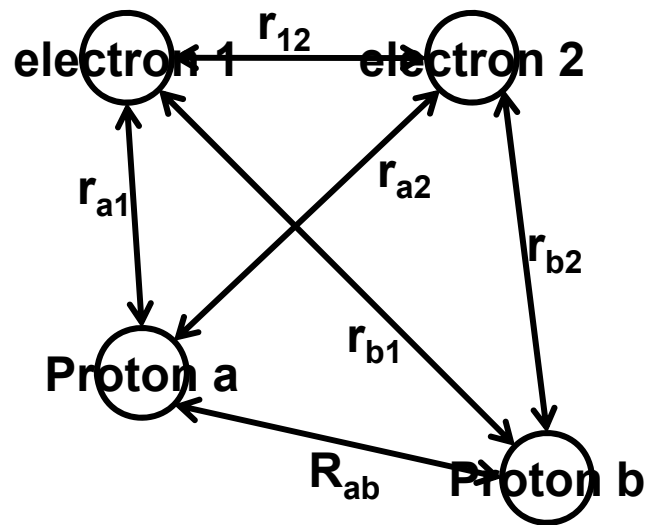


Bonding State (Symmetric wavefn)
Antibonding State (Antisymmetric wavefn)



The Hydrogen Molecule, H₂

$$H = -\frac{\hbar^2}{2m_0} \nabla_1^2 - \frac{e^2}{4\pi\epsilon_0 r_{a1}} - \frac{\hbar^2}{2m_0} \nabla_2^2 - \frac{e^2}{4\pi\epsilon_0 r_{b2}} - \frac{e^2}{4\pi\epsilon_0 r_{b1}} - \frac{e^2}{4\pi\epsilon_0 r_{a2}} - \frac{e^2}{4\pi\epsilon_0 R_{ab}} - \frac{e^2}{4\pi\epsilon_0 r_{12}}$$



The Hydrogen Molecule, H₂

We can get wavefunction from **variational principle**

If we in fact do not use a true eigenfunction of the ground state of the system for ψ , but rather some other wavefunction, then its corresponding energy expectation value will **always be larger** than the eigenvalue of a solution of a true eigenfunction

$$E_{trial} = \frac{\int dV \psi_{trial}^* H \psi_{trial}}{\int dV \psi_{trial}^* \psi_{trial}} \quad E_{true} = \frac{\int dV \psi_{true}^* H \psi_{true}}{\int dV \psi_{true}^* \psi_{true}}$$

$$E_{trial} \geq E_{true}$$

Electronic Structure

Approaching Methods

Molecular Orbitals will be built up using LCAO
(LCAO : Linear Combination of Atomic Orbitals)

$$\psi = \sum_r c_r \phi_r$$

Pauli Exclusion Principle

Hund's Rule

Electronic Structure

Results

The central symmetry of the Coulomb potential is removed

-> the angular momentum quantum number l is no longer a good quantum number. So a new quantization condition is introduced in molecular physics, characterised by the quantity λ .

The electrons are associated with both atoms at the same time

The electronic terms which were originally degenerate are split.

Electronic Structure

Next Stories...

Electronic Structure of Diatomic Molecule

**Electronic Structure of Polyatomic molecules
(Especially, Conjugated π -systems)**

Electronic Structure of Larger Molecules